

Optical Computing Based on Transverse Spatial Modulation of Light

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GIQSUL – Department of Physics
Federal University of Santa Catarina
Florianópolis - Brazil

May, 27th, 2021



**Mini-symposium on
Sensor Network
Localization and
Dynamical Distance
Geometry**



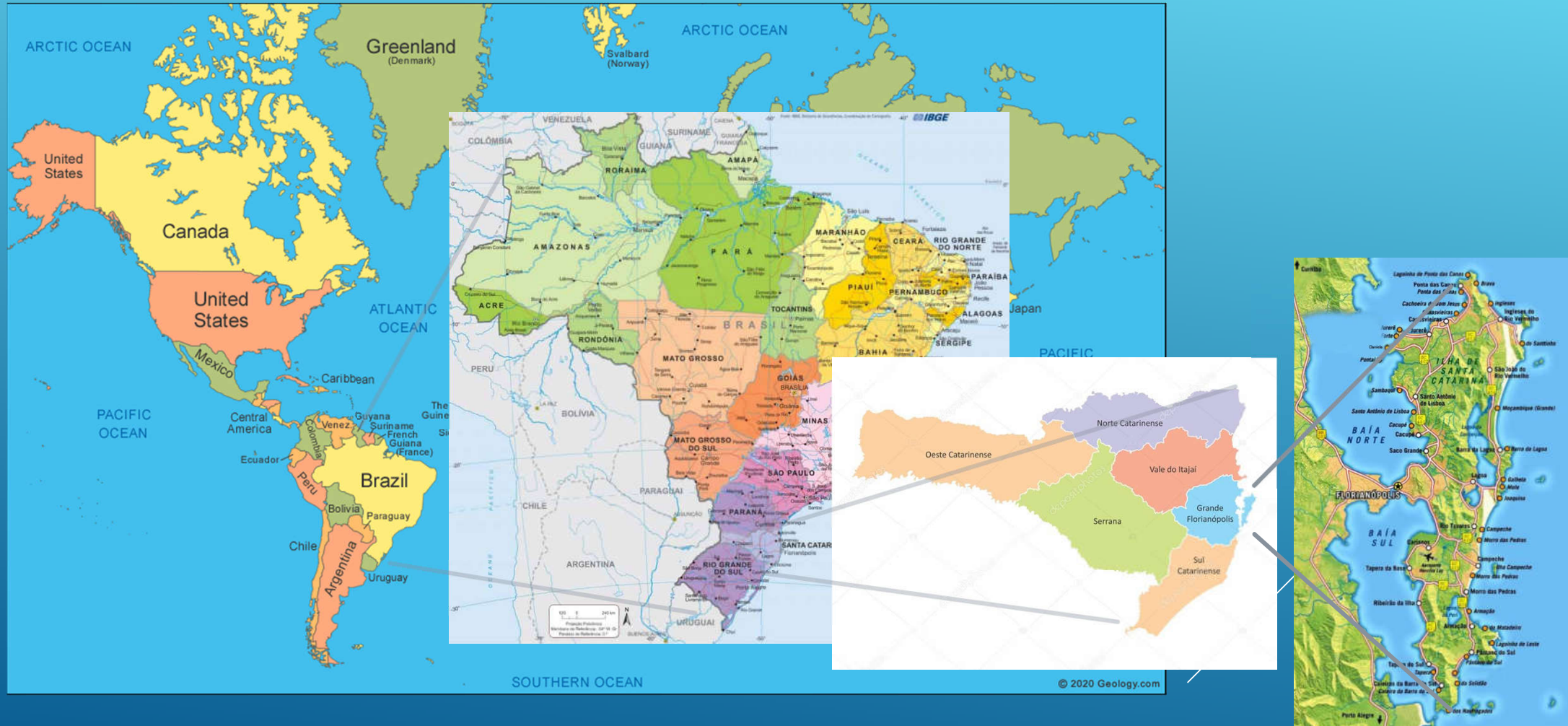


Quantum Information group GIQSUL – Federal University of Santa Catarina

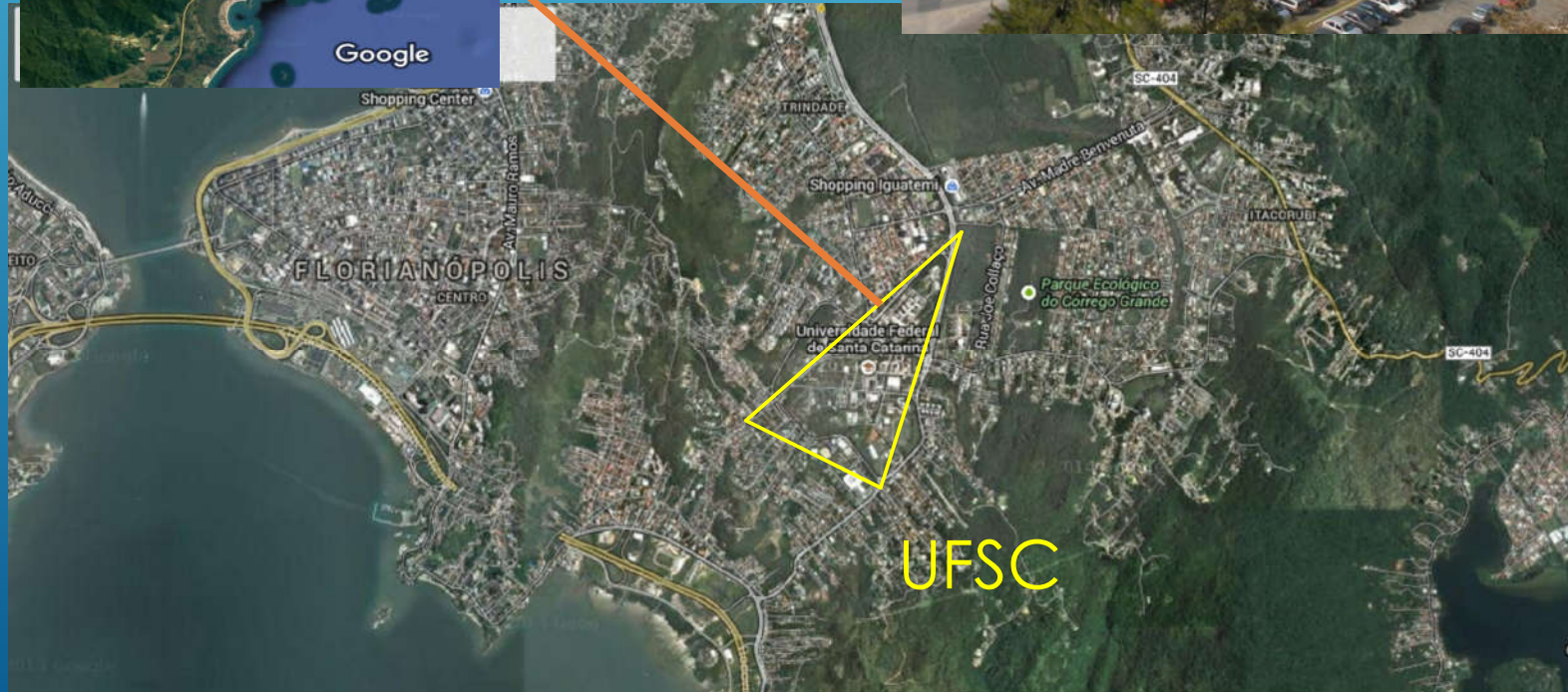
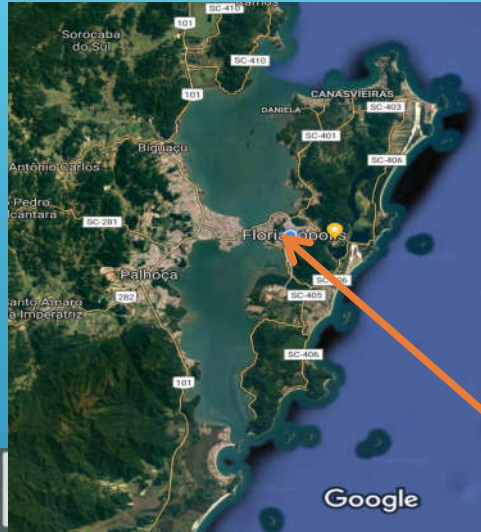


Quantum Information group GIQSUL – Federal University of Santa Catarina





Federal University of Santa Catarina UFSC



Florianópolis – SC – Brazil



Department of Physics – UFSC

GIQSUL – Optics and Quantum Information





GIQSUL

Research group on Optics and Quantum Information



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Eduardo Inácio Duzzioni
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Marcelo Felipe Zanella de Arruda
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Thomas Häffner
Gustavo Santosi
Caio Boccato Dias De Goes

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Antonio Khoury - UFF
Miles Paddgett - U. Glasgow
Martin Lavery - U. Glasgow
Rafael Gomes - UFG
Andrew Forbes - U. Witwat.
Antonio Mucherino - U. Rennes
Sérgio Muniz - USP SC
Sergei Kulik - U. Moscow
Xiasong Ma - U. Nanjing
Paula Borges Monteiro - IFSC
Willamys C. S. Silva - UFAL

Quantum Computation Quantum Advantage

2019 superconductor chip

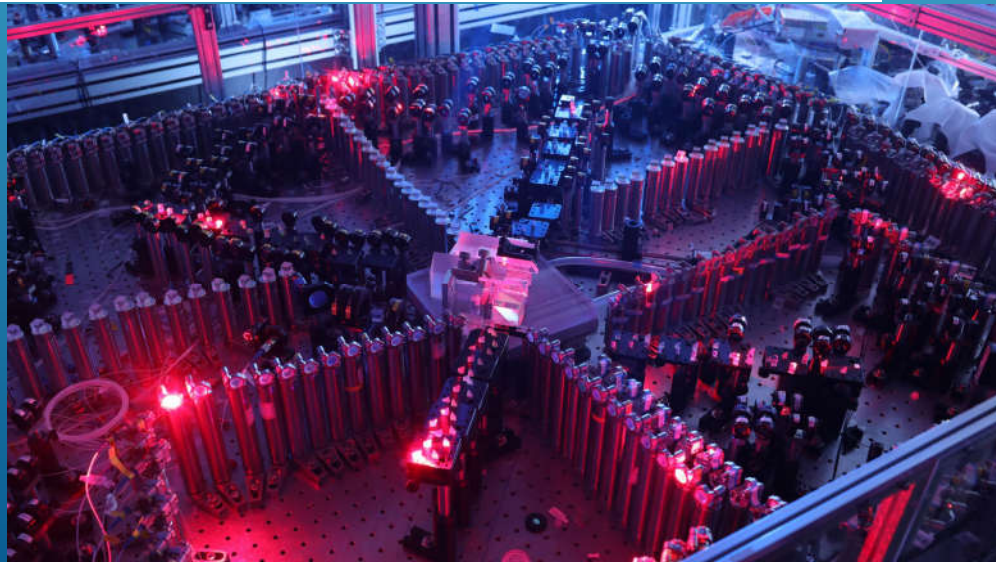
2020 Optical setup

QUANTUM COMPUTING

Quantum computational advantage using photons

Han-Sen Zhong^{1,2,*}, Hui Wang^{1,2,*}, Yu-Hao Deng^{1,2,*}, Ming-Cheng Chen^{1,2,*}, Li-Chao Peng^{1,2}, Yi-Han Luo^{1,2}, Jian Qin^{1,2}, Dian Wu^{1,2}, Xing Ding^{1,2}, Yi Hu^{1,2}, Peng Hu³, Xiao-Yan Yang³, Wei-Jun Zhang³, Hao Li³, Yuxuan Li⁴, Xiao Jiang^{1,2}, Lin Gan⁴, Guangwen Yang⁴, Lixing You³, Zhen Wang³, Li Li^{1,2}, Nai-Le Liu^{1,2}, Chao-Yang Lu^{1,2,†}, Jian-Wei Pan^{1,2,†}

Zhong *et al.*, *Science* **370**, 1460–1463 (2020) 18 December 2020



Article

Quantum supremacy using a programmable superconducting processor

<https://doi.org/10.1038/s41586-019-1666-5>

Received: 22 July 2019

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Published online: 23 October 2019

Frank Arute¹, Kunal Arya¹, Ryan Babbush¹, Dave Bacon¹, Joseph C. Bardin^{1,2}, Rami Barends¹, Rupak Biswas³, Sergio Boixo¹, Fernando G. S. L. Brandao^{1,4}, David A. Buell¹, Brian Burkett¹, Yu Chen¹, Edward J. Kim¹, Keith Gu¹, Markus J. Zhang¹, Ji Zhang¹, Dmitry I. Alexeev¹, Dmitry L. Anthony¹, Offer N. Ma¹, Andre P. Nicholas¹, Matthew Z. Jamie¹

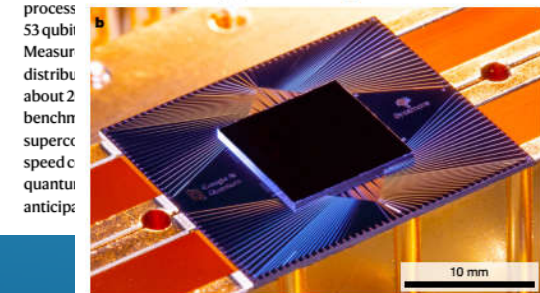
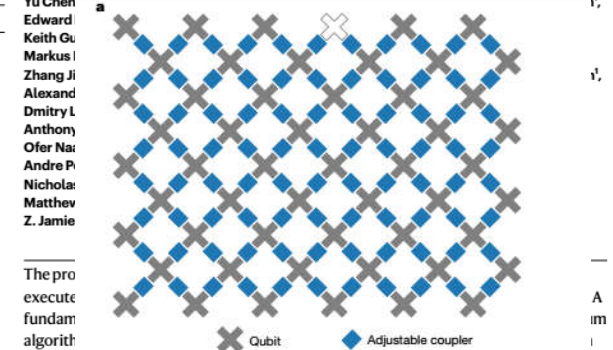


Fig. 1 | The Sycamore processor. **a**, Layout of processor, showing a rectangular array of 54 qubits (grey), each connected to its four nearest neighbours with couplers (blue). The inoperable qubit is outlined. **b**, Photograph of the Sycamore chip.

Quantum Computation Quantum Advantage

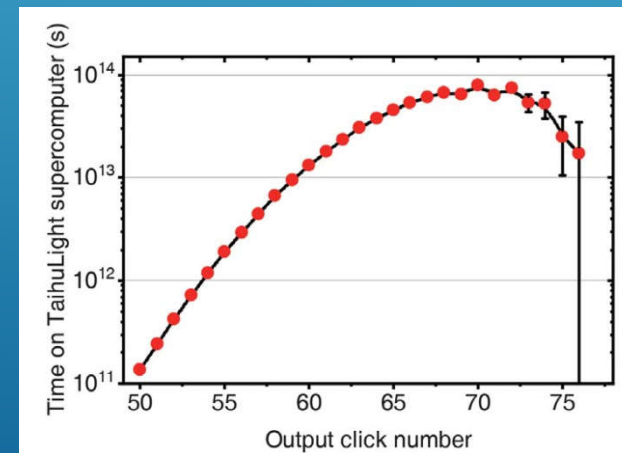
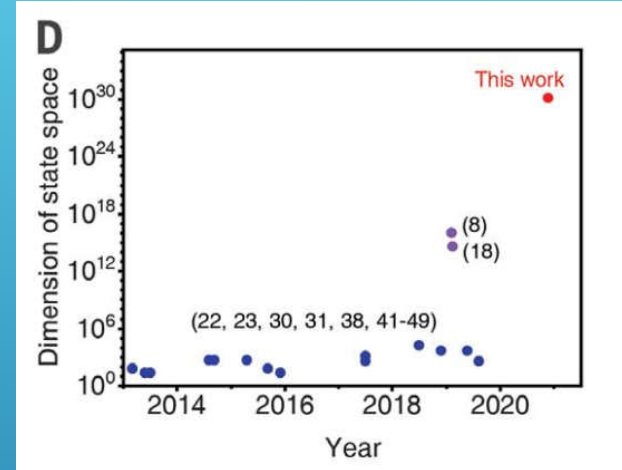
2020 Optical setup

QUANTUM COMPUTING

Quantum computational advantage using photons

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Hao Li³, Yuxuan Li⁴, Xiao Jiang^{1,2}, Lin Gan⁴, Guangwen Yang⁴, Lixing You³, Zhen Wang³, Li Li^{1,2},
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Zhong *et al.*, *Science* **370**, 1460–1463 (2020) 18 December 2020

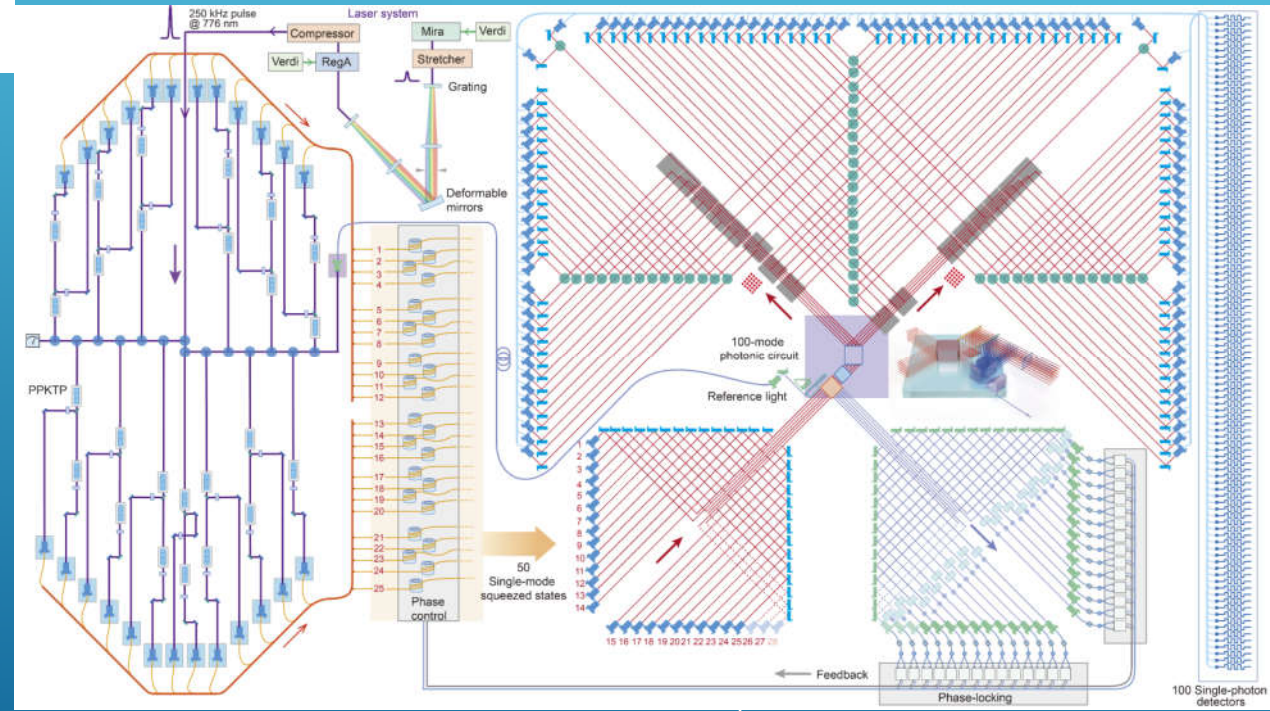


Photonic Computation Quantum Advantage

QUANTUM COMPUTING

Quantum computational advantage using photons

Han-Sen Zhong^{1,2*}, Hui Wang^{1,2*}, Yu-Hao Deng^{1,2*}, Ming-Cheng Chen^{1,2*}, Li-Chao Peng^{1,2}, Yi-Han Luo^{1,2}, Jian Qin^{1,2}, Dian Wu^{1,2}, Xing Ding^{1,2}, Yi Hu^{1,2}, Peng Hu³, Xiao-Yan Yang³, Wei-Jun Zhang³, Hao Li³, Yuxuan Li⁴, Xiao Jiang^{1,2}, Lin Gan⁴, Guangwen Yang⁴, Lixing You³, Zhen Wang³, Li Li^{1,2}, Nai-Le Liu^{1,2}, Chao-Yang Lu^{1,2†}, Jian-Wei Pan^{1,2†}



Photonic Computation Quantum Advantage/Boson Sampling

Boson Sampling on a Photonic Chip

Justin B. Spring,^{1*} Benjamin J. Metcalf,¹ Peter C. Humphreys,¹ W. Steven Kolthammer,¹
Xian-Min Jin,^{1,2} Marco Barbieri,¹ Animesh Datta,¹ Nicholas Thomas-Peter,¹ Nathan K. Langford,^{1,3}
Dmytro Kundys,⁴ James C. Gates,⁴ Brian J. Smith,¹ Peter G. R. Smith,⁴ Ian A. Walmsley^{1*}

15 FEBRUARY 2013 VOL 339 SCIENCE

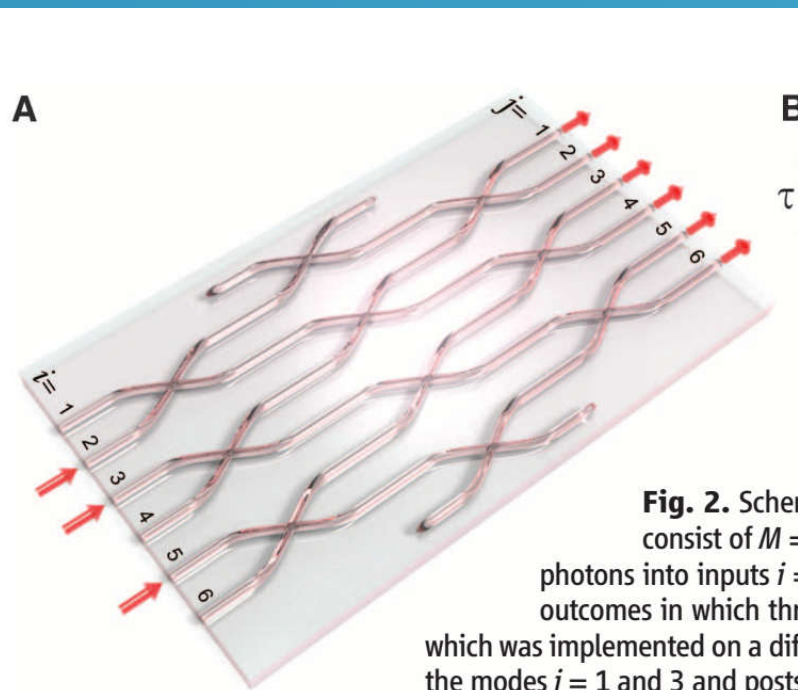


Fig. 2. Schematic of a photonic chip consisting of $M = 6$ modes. Red arrows show the paths of 3 photons into inputs $i = 1, 2, 3$ and out of outputs $j = 1, 2, 3$ which was implemented on a diffraction grating. The modes $i = 1$ and 3 and posts

3 photons
6 modes

2012

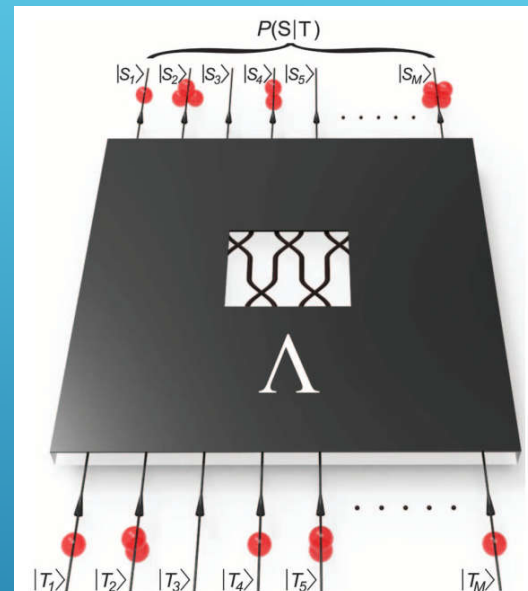


Fig. 1. Model of quantum boson sampling. Given a specified initial number state $|\mathbf{T}\rangle = |T_1 \dots T_M\rangle$ and linear transformation Λ , a QBSM efficiently samples from the distribution $P(\mathbf{S}|\mathbf{T})$ of possible outcomes $|\mathbf{S}\rangle = |S_1 \dots S_M\rangle$.

$$P(\mathbf{S}|\mathbf{T}) = |\langle \mathbf{S} | \Psi_{\text{out}} \rangle|^2 = \frac{|\text{Per}(\Lambda^{(\mathbf{S}, \mathbf{T})})|^2}{\prod_{j=1}^M S_j! \prod_{i=1}^M T_i!}$$

Photonic Computation Quantum Advantage/Boson Sampling

PHYSICAL REVIEW LETTERS **123**, 250503 (2019)

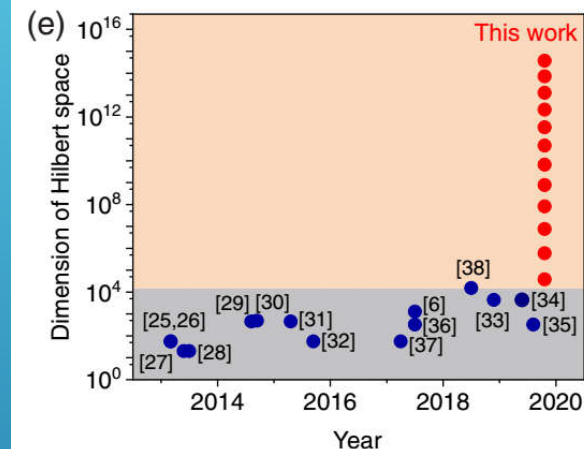
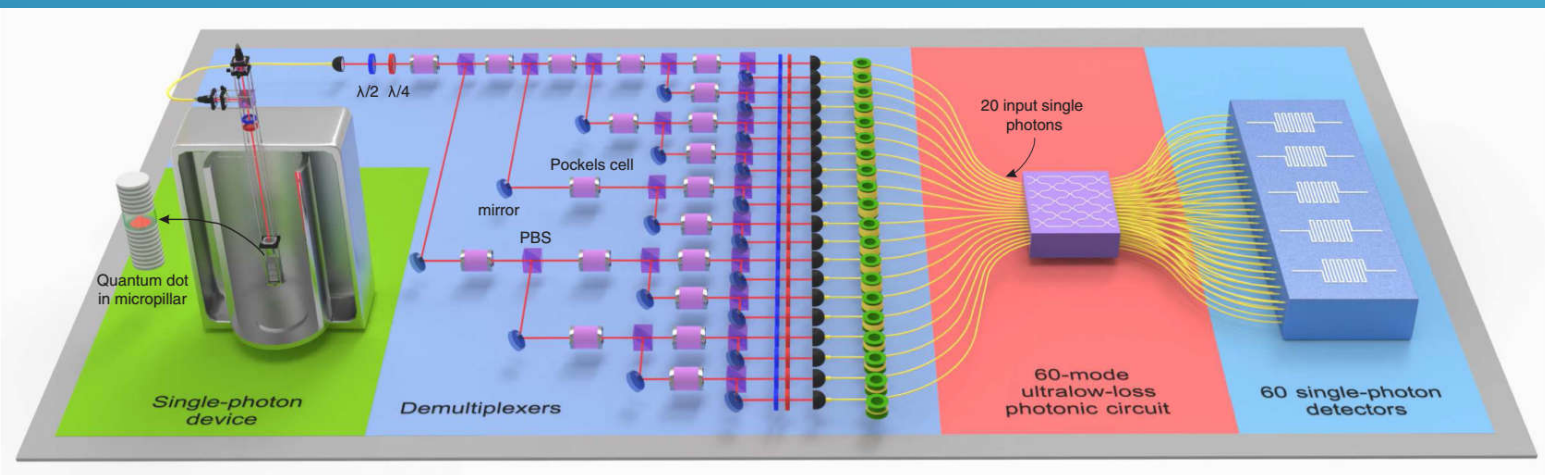
Editors' Suggestion

Featured in Physics

Boson Sampling with 20 Input Photons and a 60-Mode Interferometer in a 10^{14} -Dimensional Hilbert Space

Hui Wang,^{1,2} Jian Qin,^{1,2} Xing Ding,^{1,2} Ming-Cheng Chen,^{1,2} Si Chen,^{1,2} Xiang You,^{1,2} Yu-Ming He,^{1,2}
Xiao Jiang,^{1,2} L. You,³ Z. Wang,³ C. Schneider,⁴ Jelmer J. Renema,⁵ Sven Höfling,^{4,6,1}
Chao-Yang Lu^{1,2} and Jian-Wei Pan^{1,2}

2019



20 photons
60 modes

Photonic Computation

Gaussian Boson Sampling

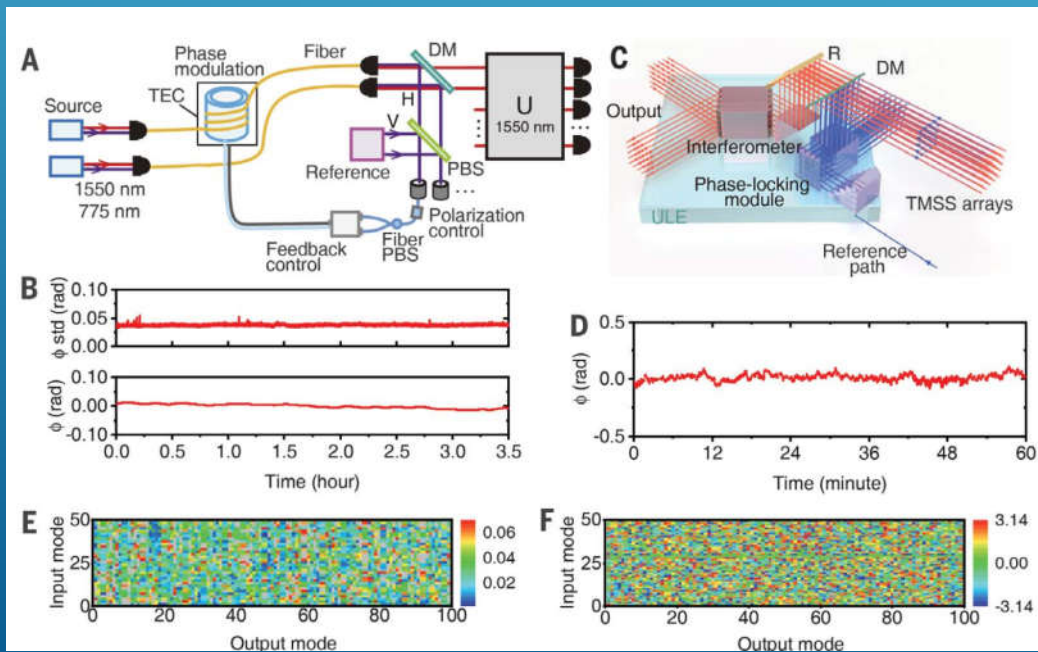
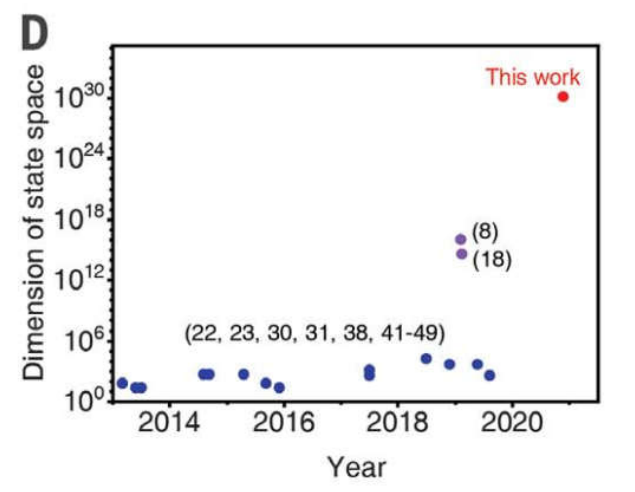
QUANTUM COMPUTING

Quantum computational advantage using photons

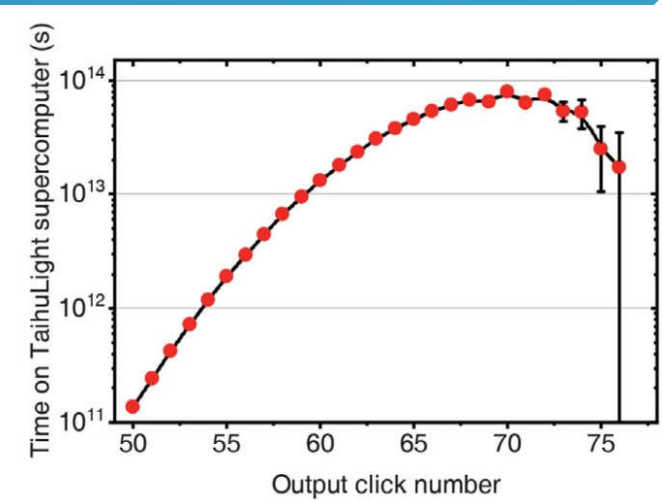
Han-Sen Zhong^{1,2*}, Hui Wang^{1,2*}, Yu-Hao Deng^{1,2*}, Ming-Cheng Chen^{1,2*}, Li-Chao Peng^{1,2}, Yi-Han Luo^{1,2}, Jian Qin^{1,2}, Dian Wu^{1,2}, Xing Ding^{1,2}, Yi Hu^{1,2}, Peng Hu³, Xiao-Yan Yang³, Wei-Jun Zhang³, Hao Li³, Yuxuan Li⁴, Xiao Jiang^{1,2}, Lin Gan⁴, Guangwen Yang⁴, Lixing You³, Zhen Wang³, Li Li^{1,2}, Nai-Le Liu^{1,2}, Chao-Yang Lu^{1,2†}, Jian-Wei Pan^{1,2†}

Zhong *et al.*, *Science* **370**, 1460–1463 (2020) 18 December 2020

2020



50 SMSS
100 modes



3-qubit Optical Quantum Simulation

PRL **112**, 160501 (2014)

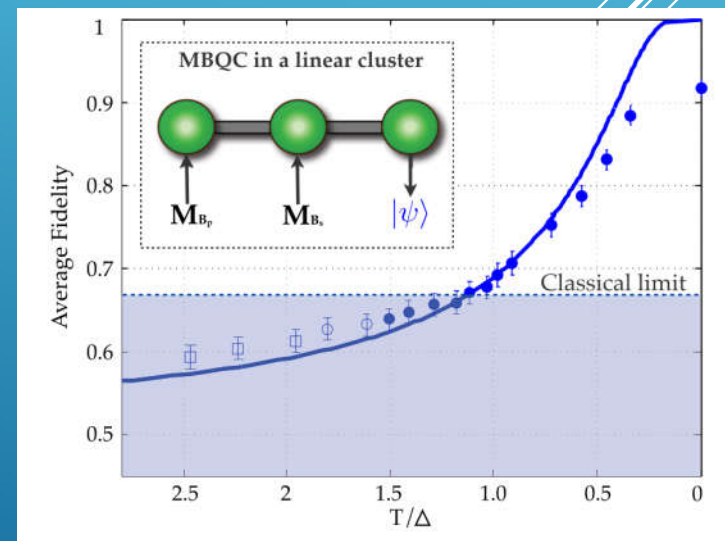
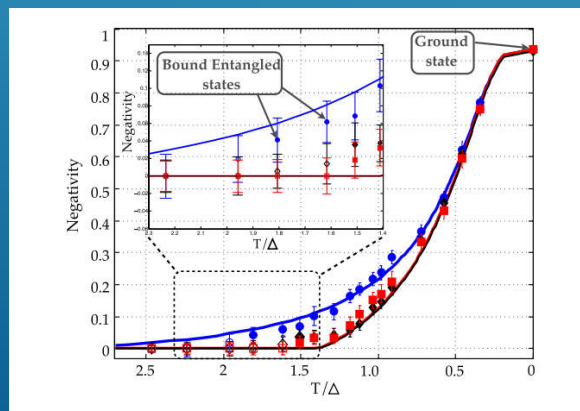
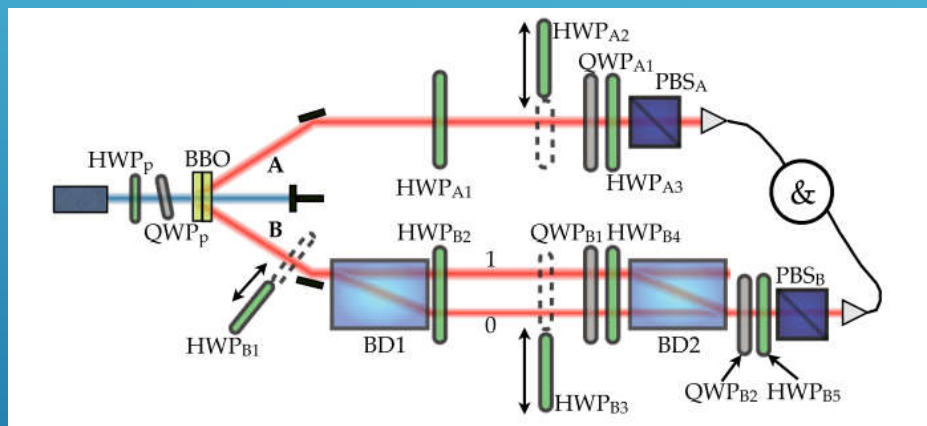
PHYSICAL REVIEW LETTERS

week ending
25 APRIL 2014



Linear-Optical Simulation of the Cooling of a Cluster-State Hamiltonian System

G. H. Aguilar,¹ T. Kolb,¹ D. Cavalcanti,² L. Aolita,³ R. Chaves,⁴ S. P. Walborn,¹ and P. H. Souto Ribeiro¹



Quantum simulation with classical light: Analogy between the paraxial wave equation and 2D Schrödinger equation

Helmholtz equation

$$\nabla^2 A + k^2 A = 0$$

$$\nabla_T^2 A + 2ik \frac{\partial A}{\partial z} = 0$$

Helmholtz paraxial equation:

Time dependent Schrödinger equation:

$$\nabla^2 \psi + i \frac{2m}{\hbar} \frac{\partial \psi}{\partial t} = 0$$

Quantum simulation:

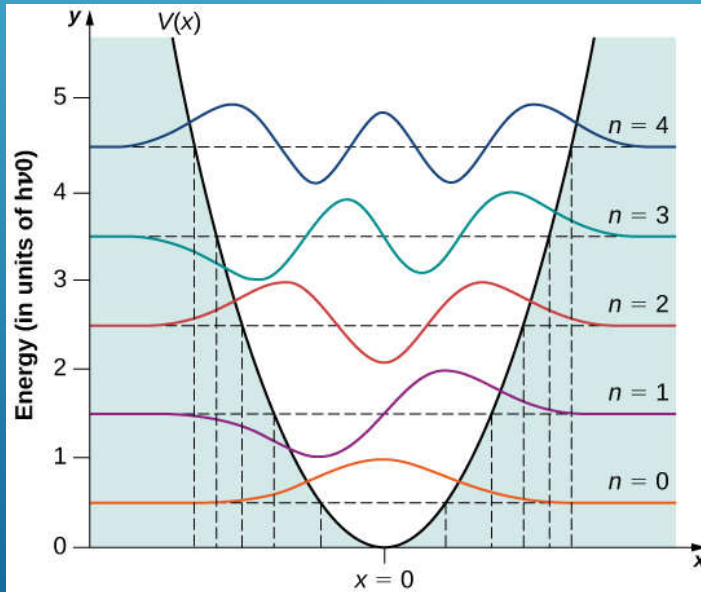
$$i\hbar \frac{\partial \psi(x,t)}{\partial t} = \left(-\hbar^2 \frac{\partial^2}{\partial x^2} + V(x) \right) \psi(x,t)$$

$$\frac{i}{k} \frac{\partial \psi(x,z)}{\partial z} = \left(-\frac{1}{2k^2} \frac{\partial^2}{\partial x^2} + n(x) \right) \psi(x,z)$$

$$n(x) = n_0 - \frac{1}{2} n_1 x^2$$

Quantum simulation with classical light: Analogy between the paraxial wave equation and 2D Schrödinger equation

Quantum Harmonic Oscillator



$$\frac{i}{k} \frac{\partial \psi(x, z)}{\partial z} = \left(-\frac{1}{2k^2} \frac{\partial^2}{\partial x^2} + n(x) \right) \psi(x, z)$$
$$n(x) = n_0 - \frac{1}{2} n_1 x^2$$

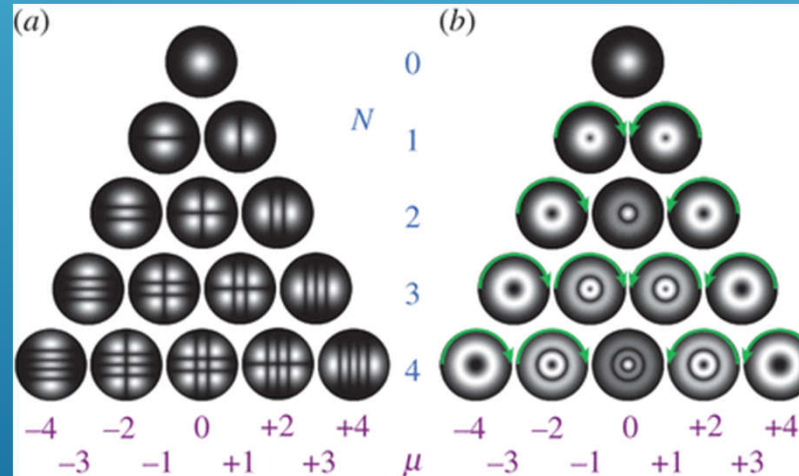


Figure credits:

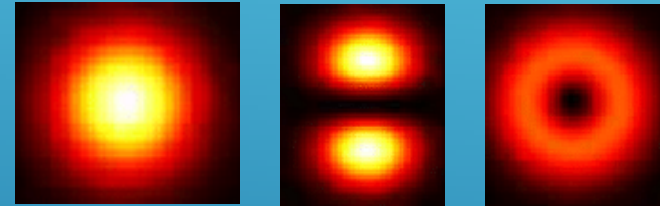
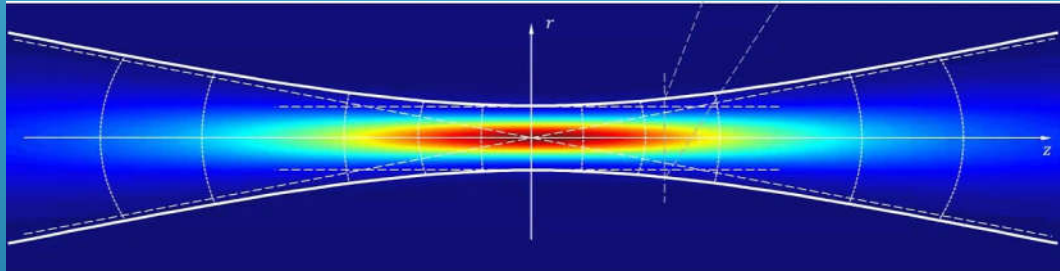
Phil. Trans. R. Soc. A

Swings and roundabouts: optical Poincaré spheres for polarization and Gaussian beams, M. R. Dennis, M. A. Alonso,

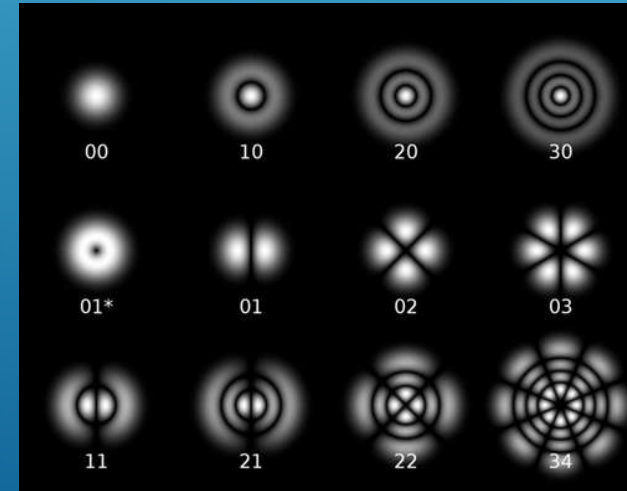
DOI: 10.1098/rsta.2015.0441

Quantum simulation with classical light: Analogy between the paraxial wave equation and 2D Schrödinger equation

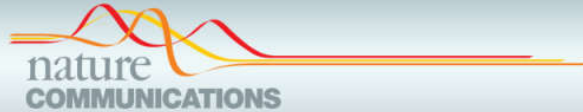
Gaussian beams



Laguerre-Gaussian beams, Hermite-Gaussian beams and linear combinations



Quantum Simulation Using Classical Light



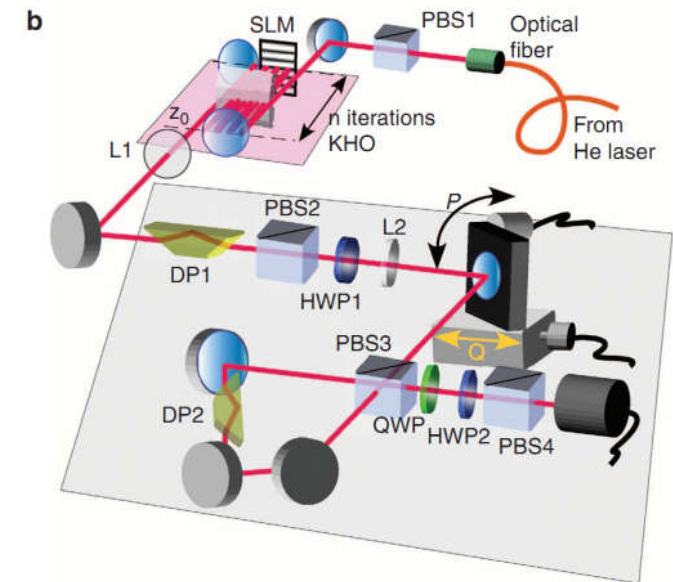
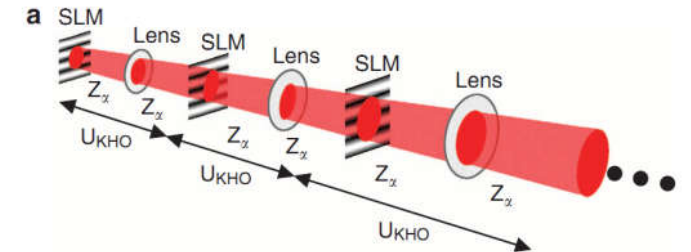
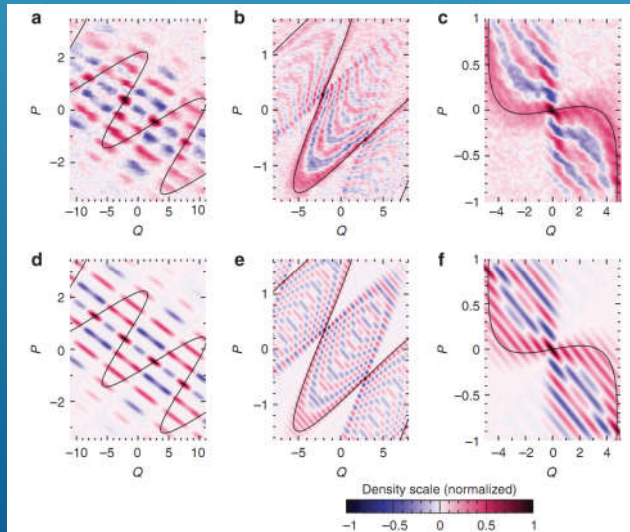
ARTICLE

Received 18 Sep 2012 | Accepted 19 Oct 2012 | Published 20 Nov 2012

DOI: 10.1038/ncomms2214

Experimental observation of quantum chaos in a beam of light

Gabriela B. Lemos¹, Rafael M. Gomes¹, Stephen P. Walborn¹, Paulo H. Souto Ribeiro¹ & Fabricio Toscano¹



Emulating a quantum harmonic oscillator to study quantum thermodynamics

J. Phys. Commun. **2** (2018) 035012

<https://doi.org/10.1088/2399-6528/aab178>

Journal of Physics Communications

PAPER

Experimental study of quantum thermodynamics using optical vortices

R Medeiros de Araújo¹, T Häffner¹, R Bernardi¹, D S Tasca², M P J Lavery³, M J Padgett⁴, A Kanaan¹, L C Céleri⁵ and P H Souto Ribeiro^{1,6}

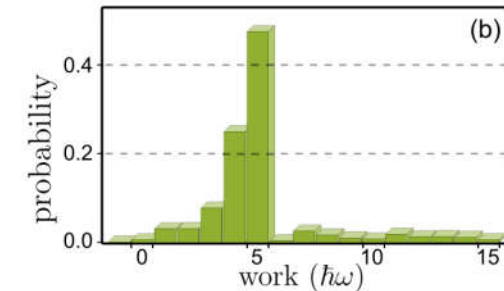
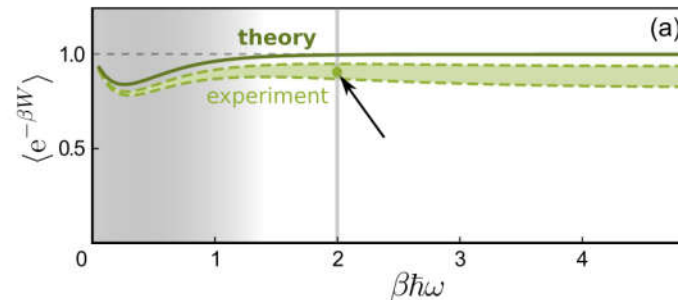
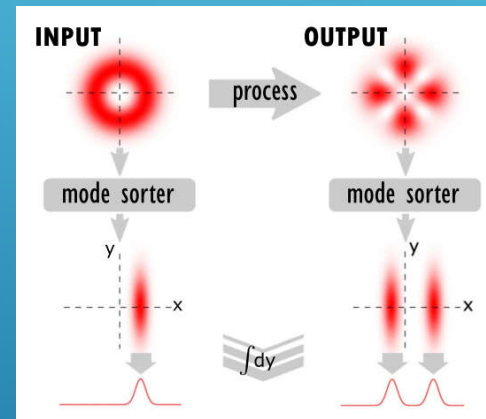
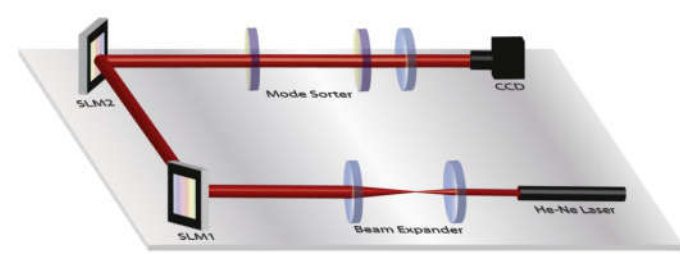
$$H = (N_r + N_l + 1) \hbar \omega$$

$$L_z = (N_r - N_l) \hbar$$

$$\text{Energy: } \varepsilon_{\ell p} = (|\ell| + 2p + 1) \hbar \omega$$

$$\text{Angular momentum: } \lambda_{\ell} = \hbar \ell$$

$$\varepsilon_{\ell} = (|\ell| + 1) \hbar \omega$$

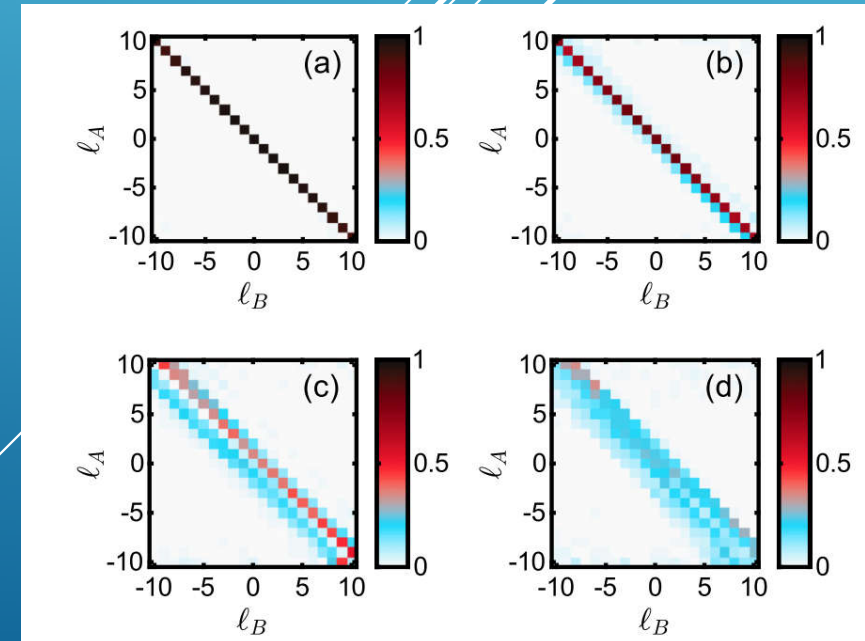
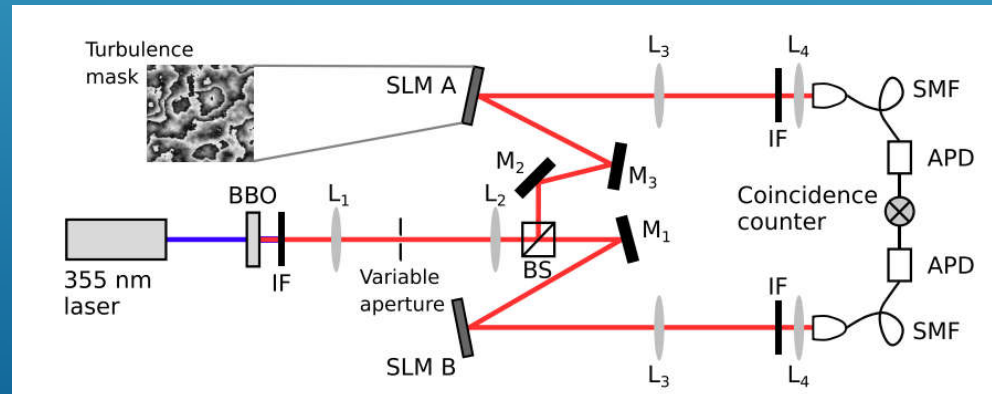


Experimental study of quantum thermodynamics using entangled photons

PHYSICAL REVIEW A **101**, 052113 (2020)

Experimental study of the generalized Jarzynski fluctuation relation using entangled photons

P. H. Souto Ribeiro,^{1,*} T. Häffner,¹ G. L. Zanin,¹ N. Rubiano da Silva¹, R. Medeiros de Araújo¹, W. C. Soares²,
R. J. de Assis,³ L. C. Céleri,^{3,4,†} and A. Forbes^{5,‡}



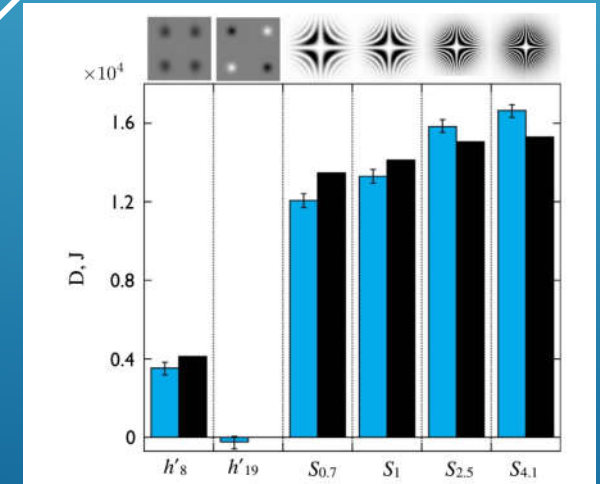
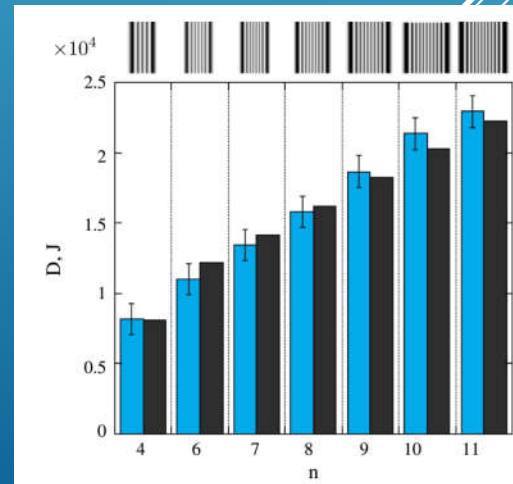
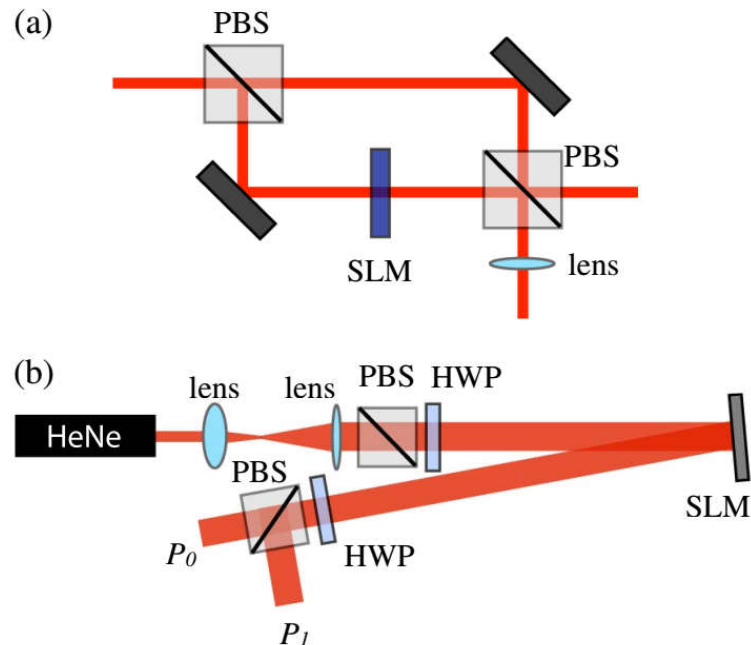
Optical integration

J. Opt. Soc. Am. A / Vol. 31, No. 4 / April 2014

Lemos *et al.*

Optical integration of a real-valued function by measurement of a Stokes parameter

G. B. Lemos,^{1,2,3,*} P. H. Souto Ribeiro,¹ and S. P. Walborn¹



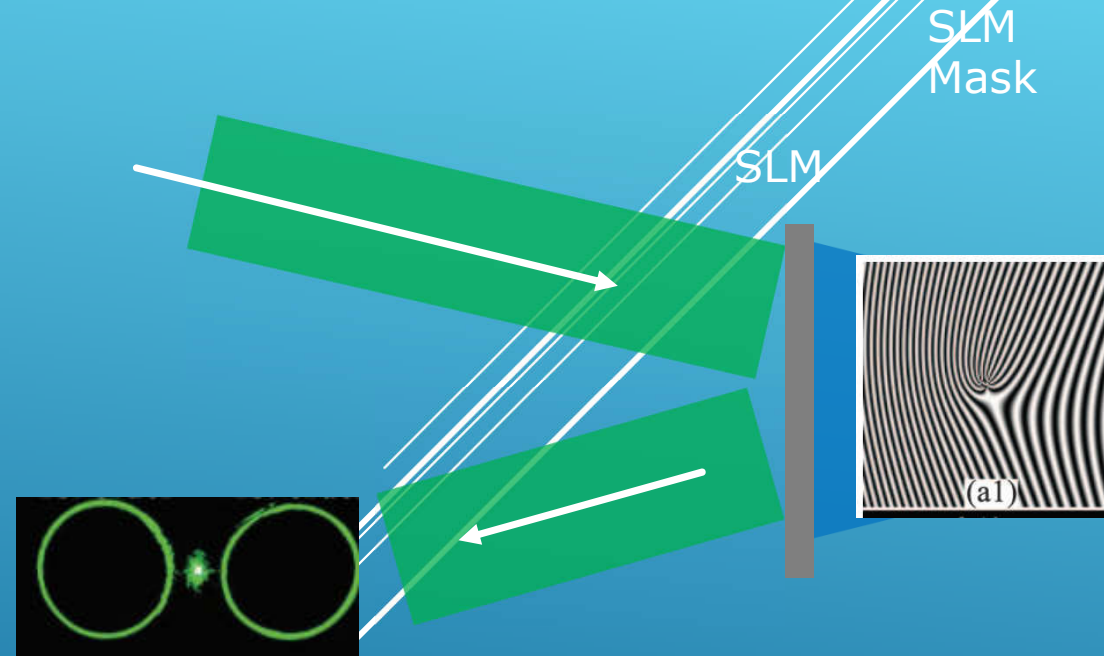
SLM



Laser projection based on
SLM (*Holoeye Photonics AG*)

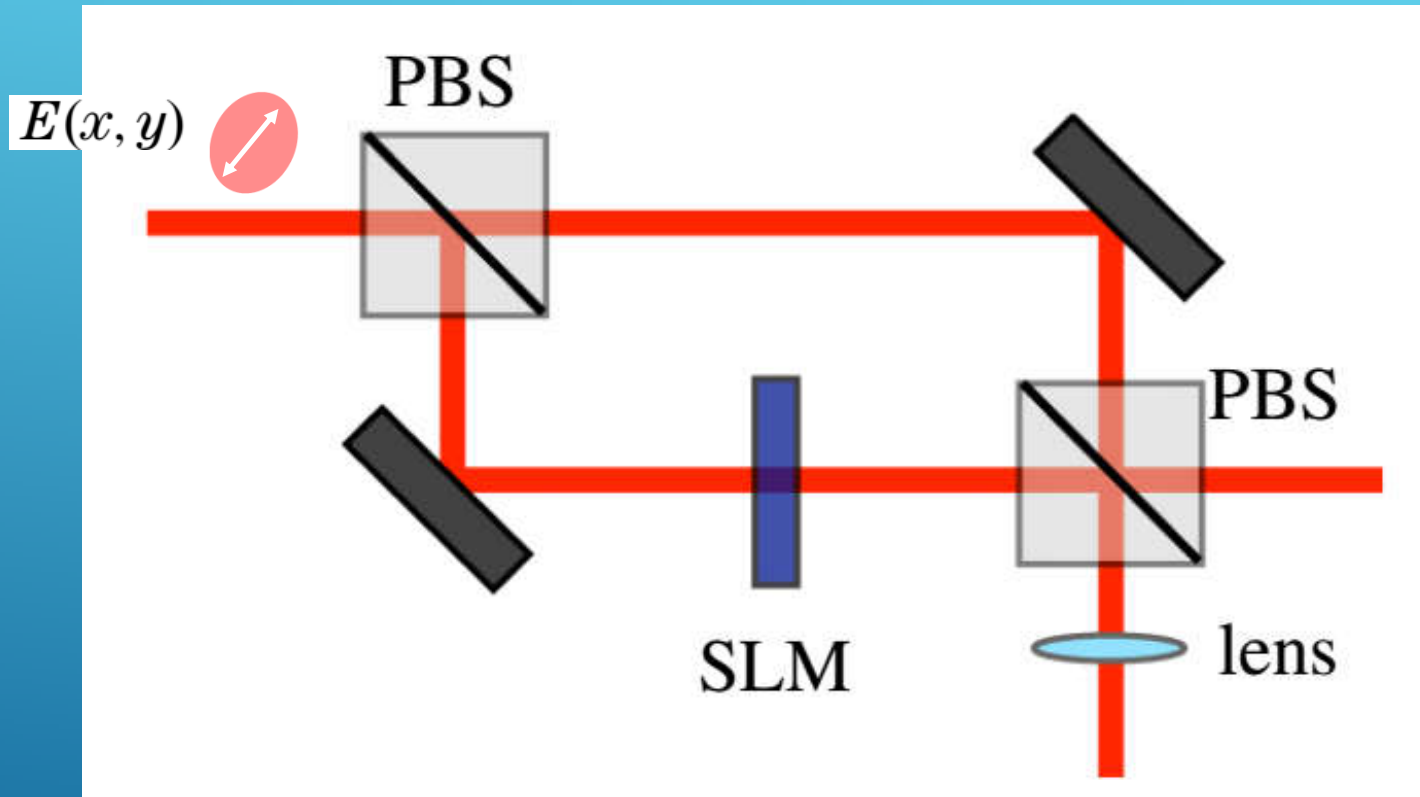


Spatial Light Modulator

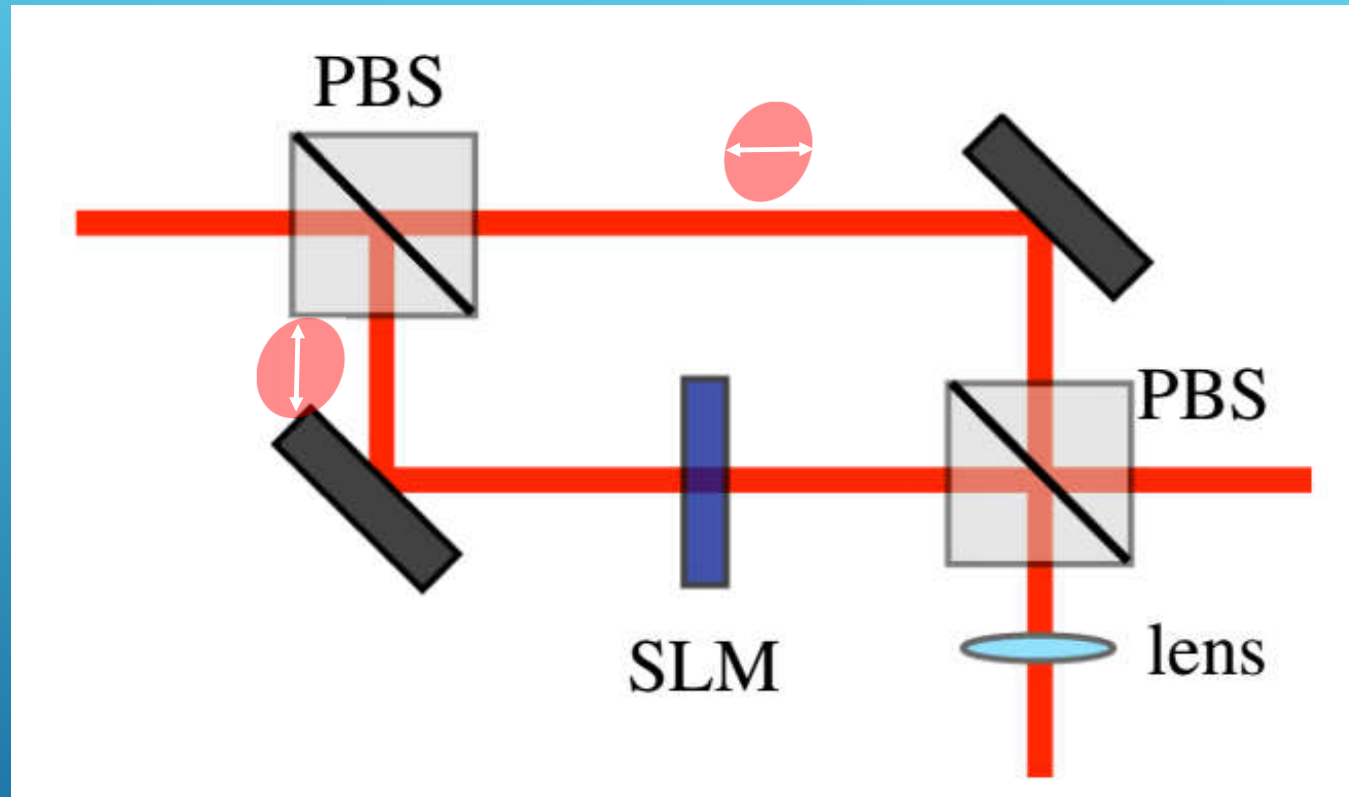


HAIXIANG MA, et al.
Vol. 42, No. 1 / January 1 2017 / Optics Letters

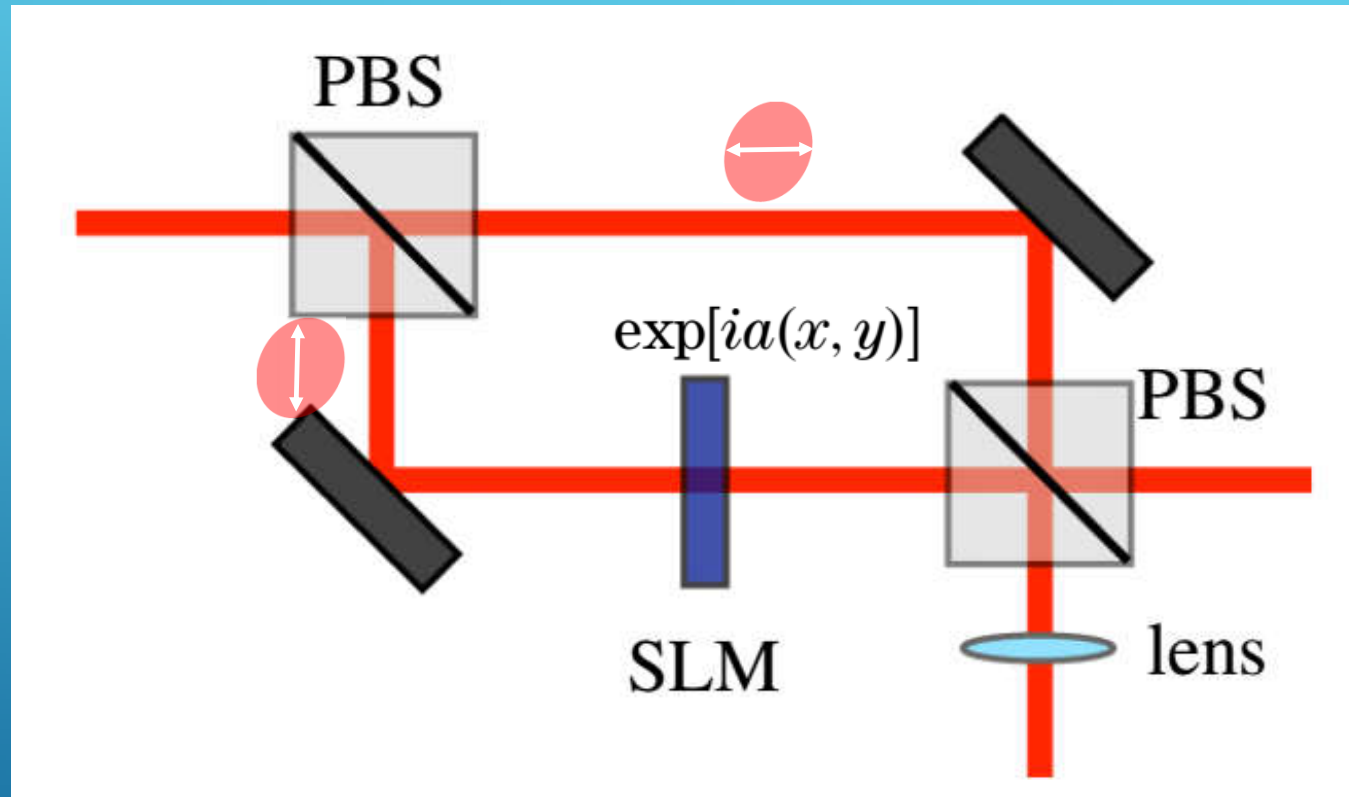
Optical integration



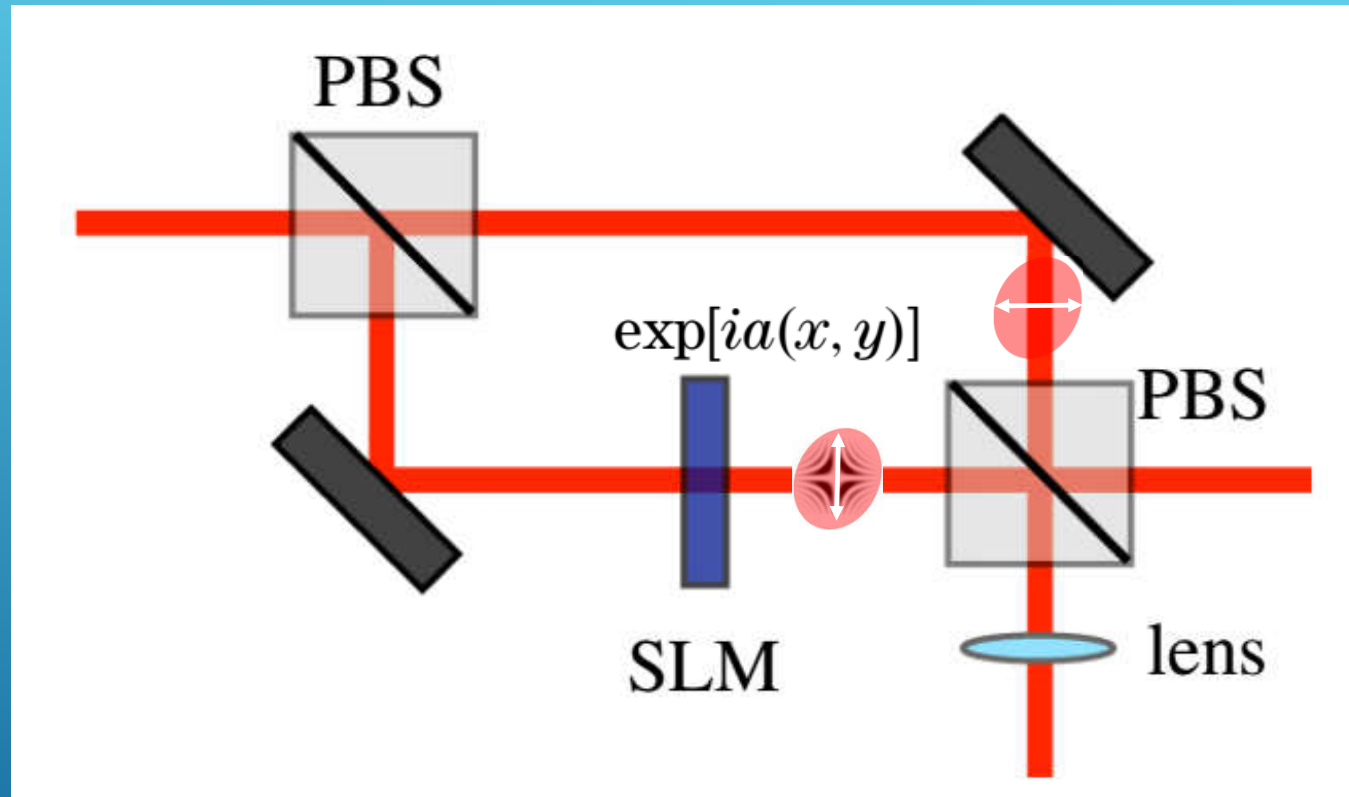
Optical integration



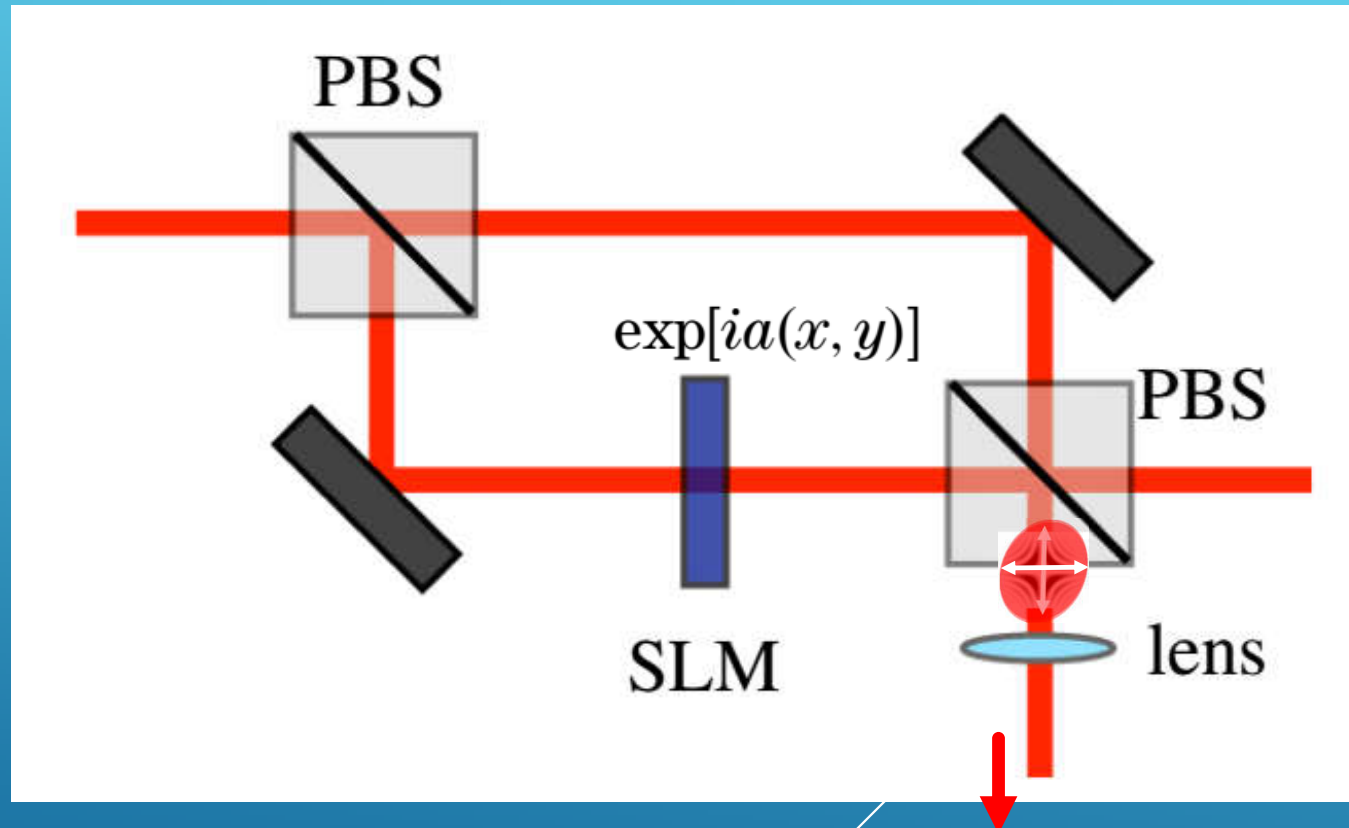
Optical integration



Optical integration

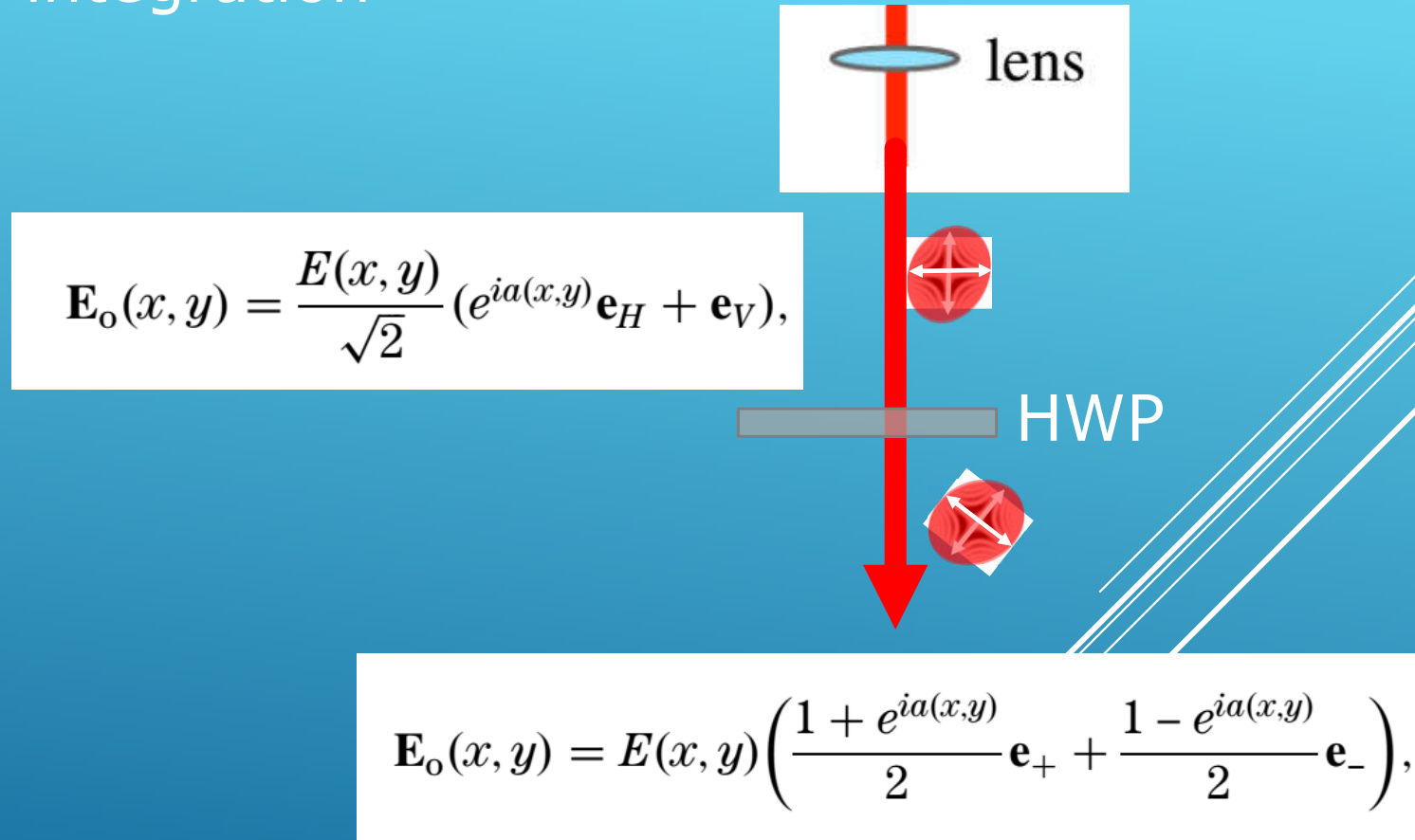


Optical integration



$$\mathbf{E}_o(x, y) = \frac{E(x, y)}{\sqrt{2}} (e^{ia(x, y)} \mathbf{e}_H + \mathbf{e}_V),$$

Optical integration



Optical integration

$$\mathbf{E}_o(x, y) = \frac{E(x, y)}{\sqrt{2}} (e^{ia(x, y)} \mathbf{e}_H + \mathbf{e}_V),$$



$$\mathbf{E}_o(x, y) = E(x, y) \left(\frac{1 + e^{ia(x, y)}}{2} \mathbf{e}_+ + \frac{1 - e^{ia(x, y)}}{2} \mathbf{e}_- \right),$$

$$I_{\pm} = \iint |E(x, y)|^2 \left\{ \frac{1}{2} \pm \frac{1}{4} (e^{ia(x, y)} + e^{-ia(x, y)}) \right\} dx dy,$$

$$I_{\pm} = \iint |E(x, y)|^2 \frac{1}{2} \{ 1 \pm \cos[a(x, y)] \} dx dy.$$



Det1 : I_+



Det2 : I_-

Optical integration

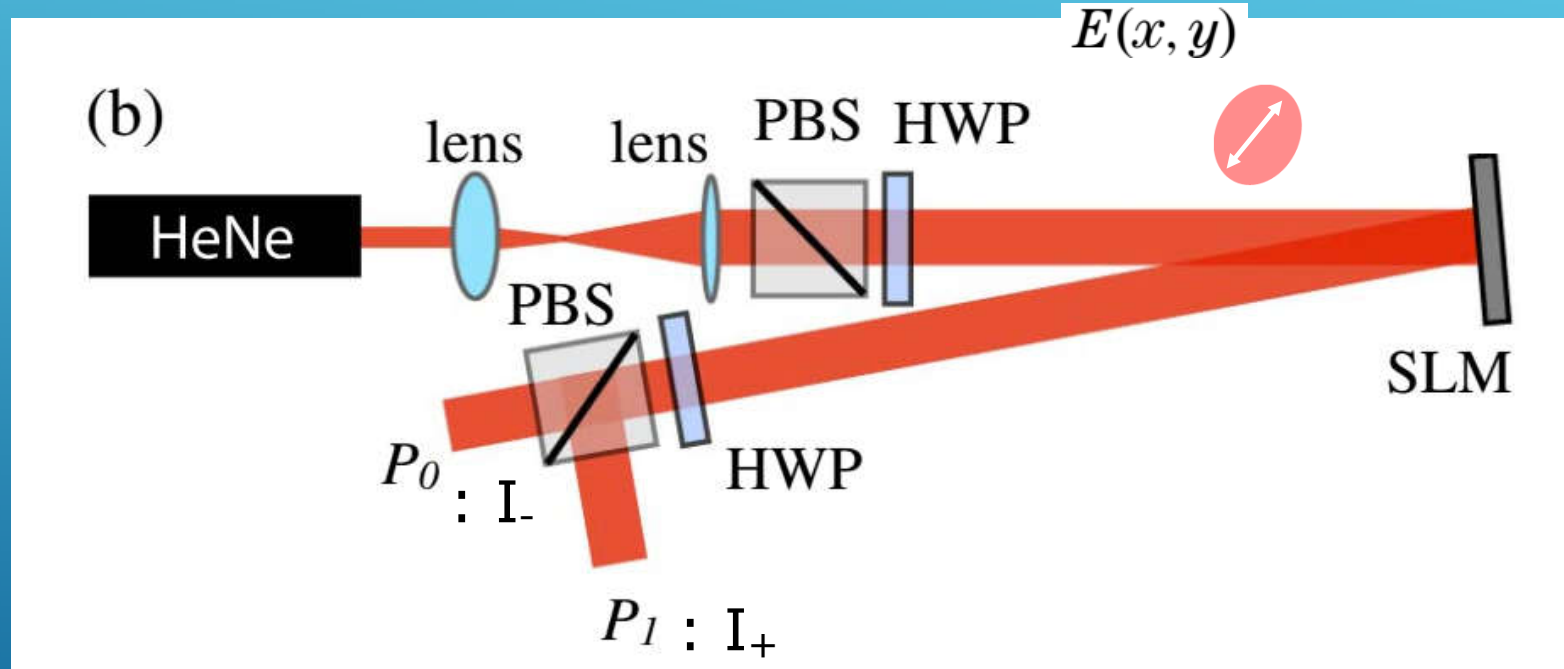
$$I_{\pm} = \iint |E(x, y)|^2 \frac{1}{2} \{1 \pm \cos[a(x, y)]\} dx dy.$$

$$a(x, y) = \arccos[f(x, y)],$$

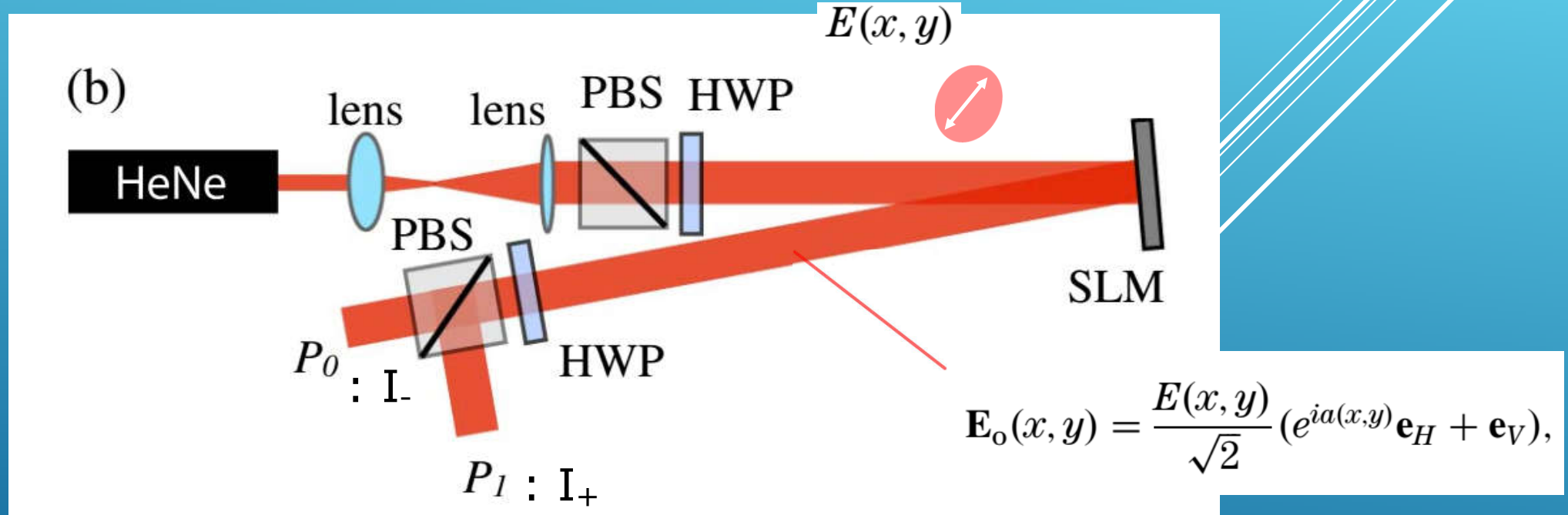
$$D = \iint |E(x, y)|^2 f(x, y) dx dy.$$

$$D = I_+ - I_-$$

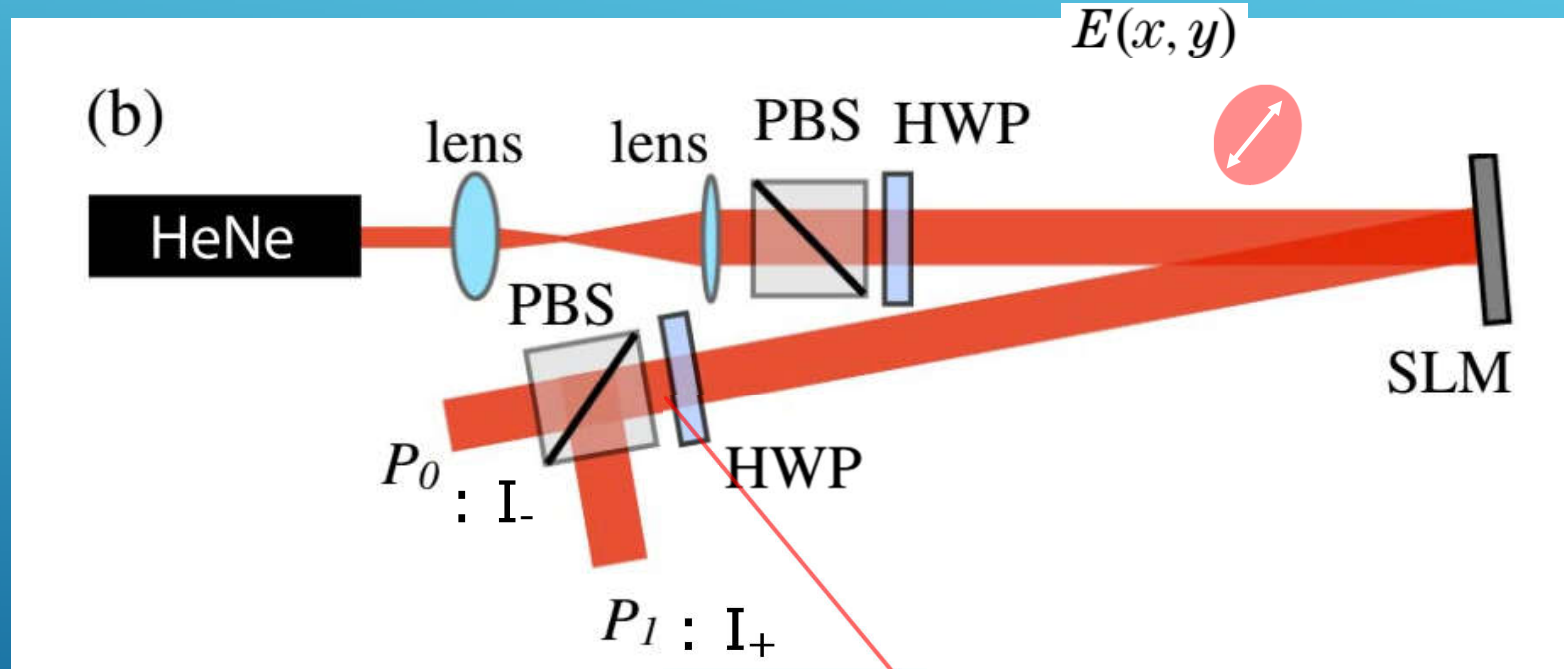
Optical integration using reflective SLM



Optical integration using reflective SLM

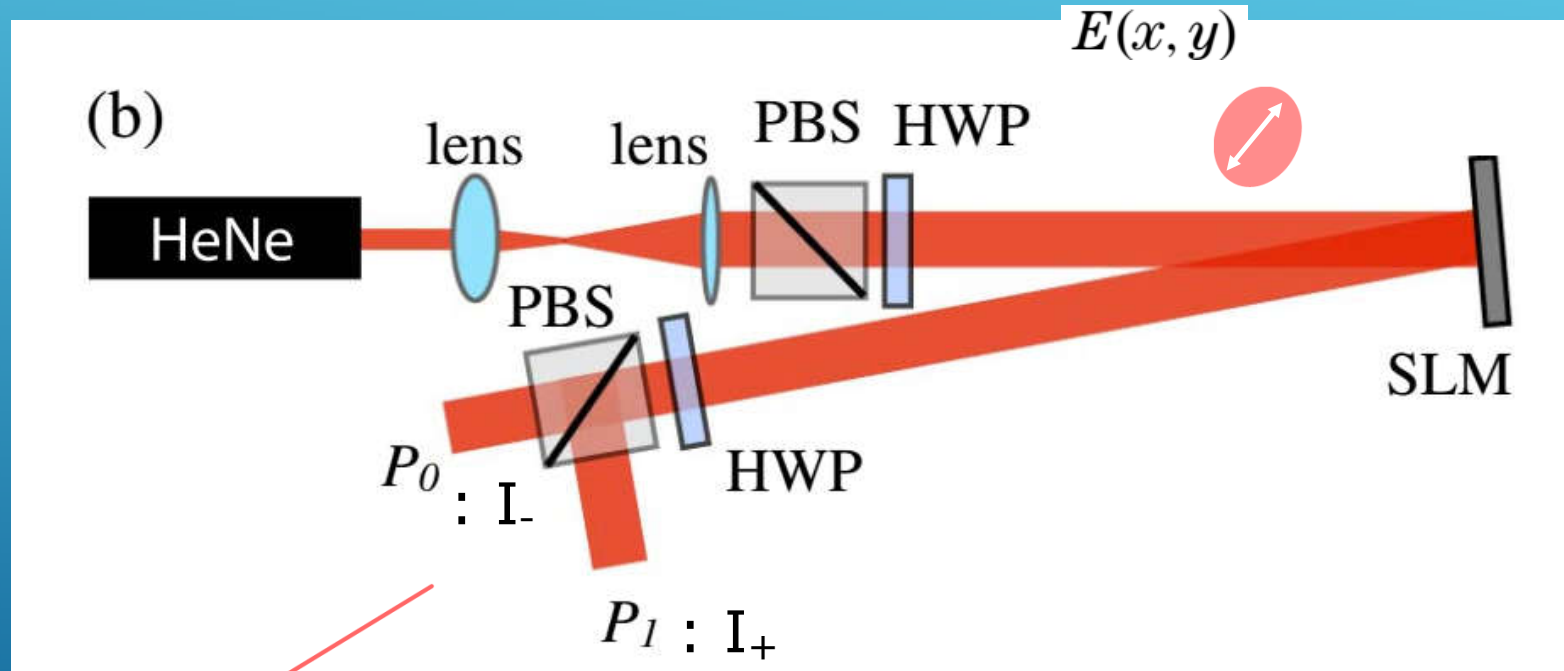


Optical integration using reflective SLM



$$\mathbf{E}_o(x, y) = E(x, y) \left(\frac{1 + e^{ia(x, y)}}{2} \mathbf{e}_+ + \frac{1 - e^{ia(x, y)}}{2} \mathbf{e}_- \right),$$

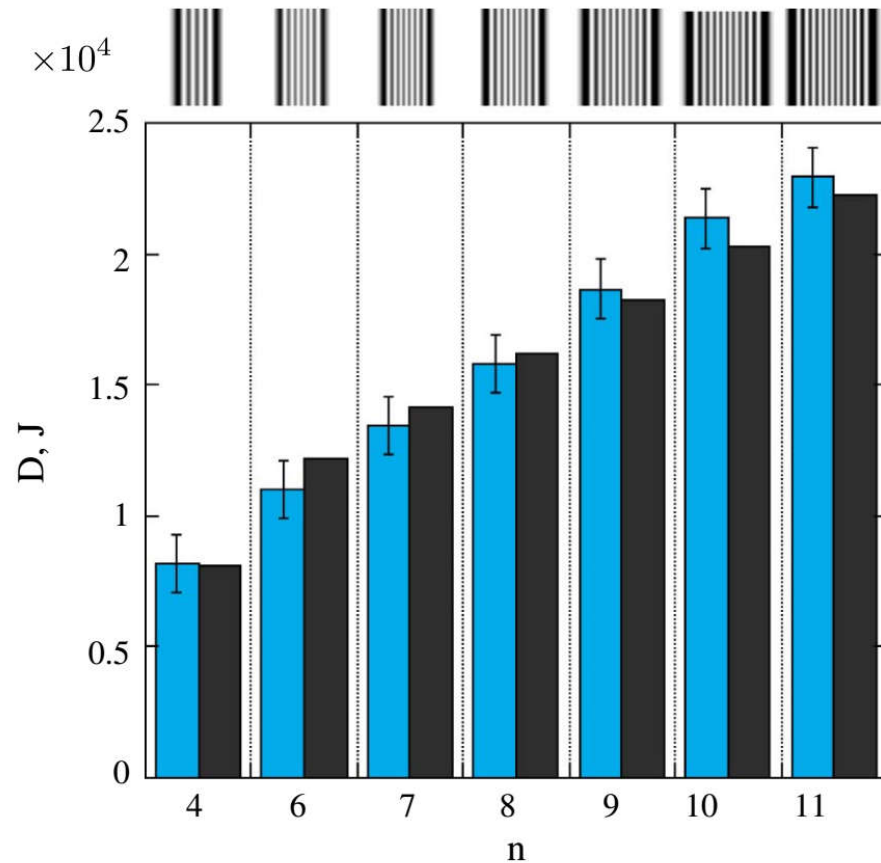
Optical integration using reflective SLM



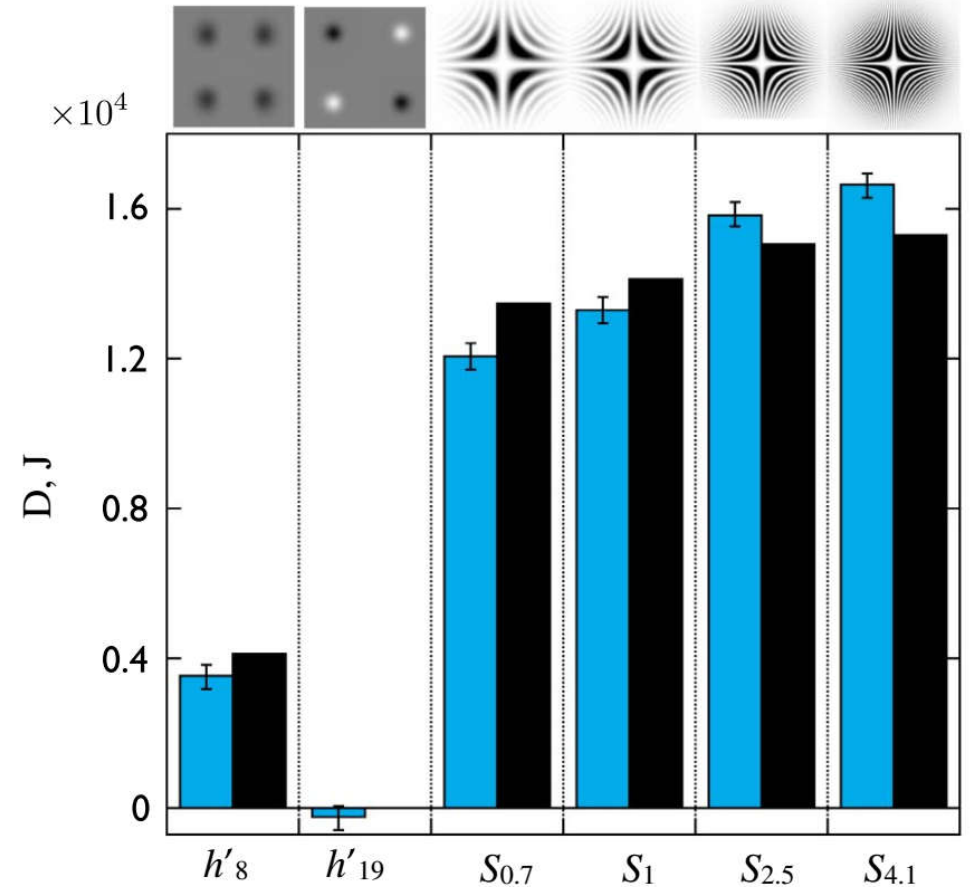
$$I_{\pm} = \iint |E(x, y)|^2 \frac{1}{2} \{1 \pm \cos[a(x, y)]\} dx dy.$$

Examples of optical integration

1D functions



2D functions

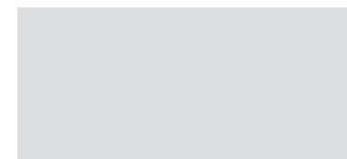
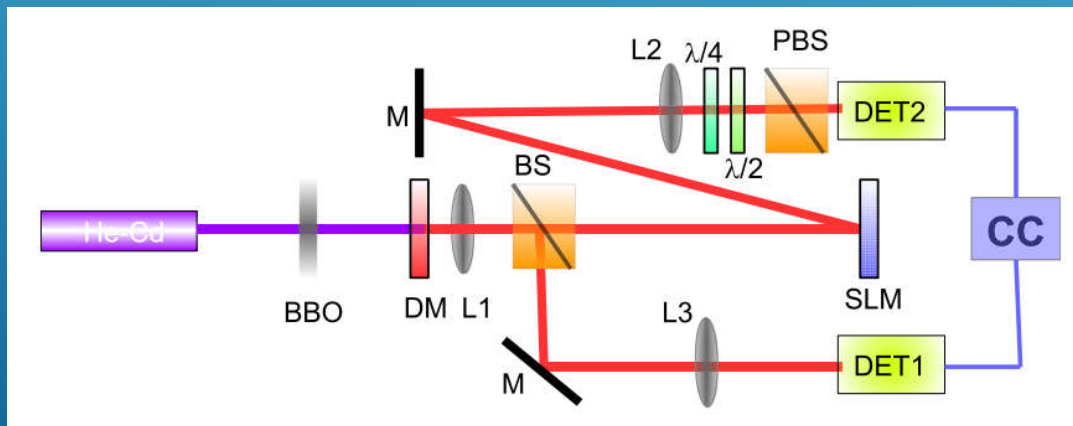


Optical computation of a quantum algorithm: Deutsch-Jozsa

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Deterministic quantum computation with one photonic qubit

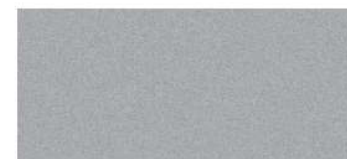
M. Hor-Meyll, D. S. Tasca, S. P. Walborn, and P. H. Souto Ribeiro*



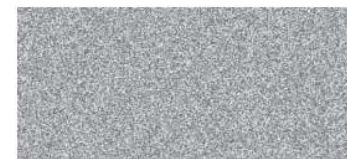
Constant, $\phi = 0$
 $\langle \sigma_x \rangle = 0.92$



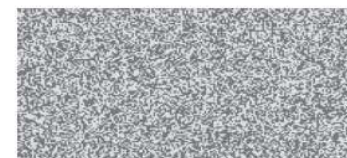
Constant, $\phi = \pi$
 $\langle \sigma_x \rangle = -0.94$



Balanced, 1 pixel
 $\langle \sigma_x \rangle = 0.19$



Balanced, 5 pixels
 $\langle \sigma_x \rangle = -0.04$



Balanced, 10 pixels
 $\langle \sigma_x \rangle = -0.01$

What about Dynamical Distance Geometry?

Solving the One-dimensional Distance Geometry Problem by Optical Computing

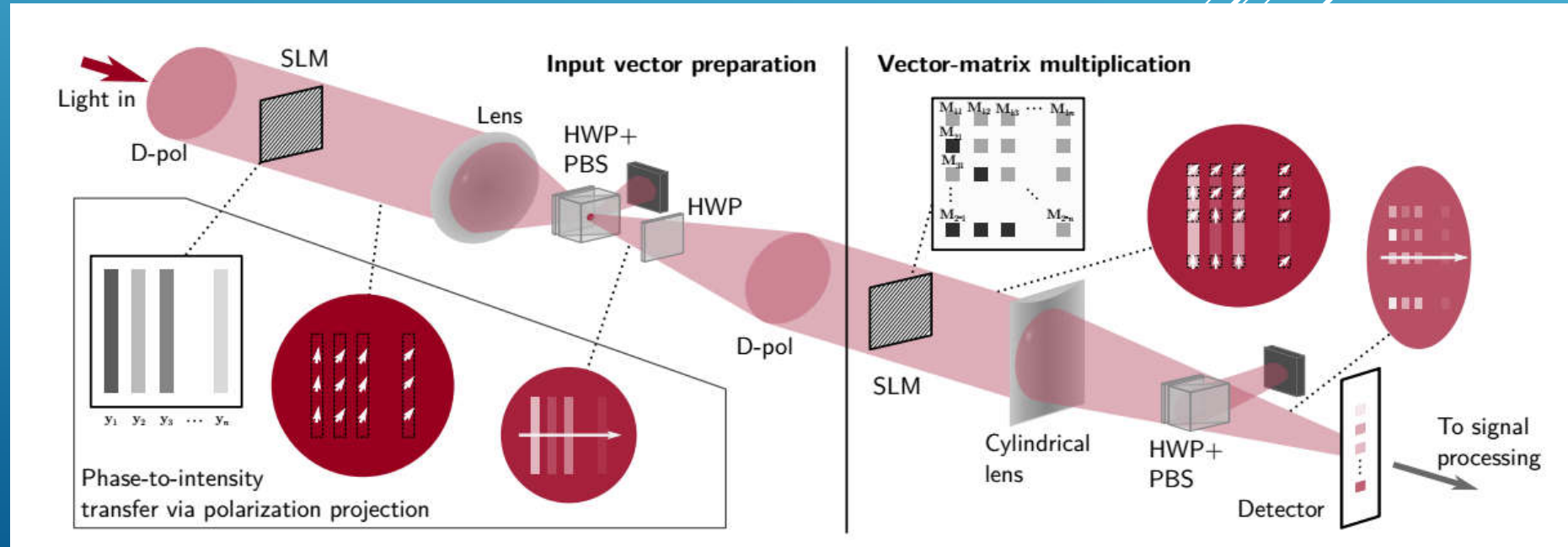
S.B. Hengeveld,^{1,*} N. Rubiano da Silva,^{2,†} D. S. Gonçalves,^{3,‡} P. H. Souto Ribeiro,^{2,§} and A. Mucherino^{1,¶}

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arXiv:2105.12118v1 [cs.ET] 25 May 2021



Thank you!

A series of five parallel white lines of varying lengths, slanted diagonally from the bottom-left towards the top-right, located in the lower-right quadrant of the slide.