# THE FIELDS INSTITUTE

FOR RESEARCH IN MATHEMATICAL SCIENCES

ABSTRACTS 1.2

# JEAN-LOUIS COLLIOT-THLNE Universite de Paris-Sud

#### Cycles algbriques et cohomologie tale

Rsum : On rappellera plusieurs contributions de Spencer Bloch l'tude des cycles algbriques (en particulier cycles de torsion et corps de classes suprieur) et on voquera quelques-uns de leurs dveloppements au cours des trente dernires annes.

#### HLNE ESNAULT Universitt Duisburg-Essen

#### Remarks and questions on coniveau

S. Bloch decomposed the diagonal on complex surfaces with trivial Chow group of 0cycles in order to show Mumford's theorem asserting that the corner piece of the Hodge filtration dies. We shall review how we could use this idea, together with Deligne's integrality theorem, in order to find rational points over finite fields. We shall show what is precisely the obstruction to use this method in order to understand abstract singular varieties, and, most specifically, mod p reduction of varieties defined over local fields. We shall review questions and remarks on this.

#### ERIC M. FRIEDLANDER Northwestern University

Musings about algebraic cycles modulo algebraic equivalence

tba

### ALEXANDER GONCHAROV Brown University

Motivic fundamental groups of curves and Feynman integrals

tba

### LUC ILLUSIE Universite Paris-Sud

On Gabber's recent work in étale cohomology

Gabber has recently solved basic open problems in étale cohomology dating back to SGA 4 and SGA 5, such as the constructibility of direct images of constructible sheaves of torsion prime to the characteristics by morphisms of finite type between excellent schemes. I will give a survey of his results and an outline of the strategy of their proofs.

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### KAZUYA KATO Kyoto University

Non-commutative Iwasawa theory and Hilbert modular forms

The best thing in my life in the study was that in the joint work with Spencer Bloch, we formulated so called Tamagawa number conjecture on L-functions of motives. This conjecture is now generalized to the equivariant version which is understood as non-commutative Iwasawa theory of motives. In my talk, I will show how to prove a very special case of the main conjecture of the non-commutative Iwasawa theory of totally real fields.

### MARC LEVINE Northeastern University

### Motivic Postnikov towers

Combining the concrete approach to the Atiyah-Hirzebruch spectral sequence arising from the work of Bloch-Lichtenbaum and Friedlander-Suslin with the abstract approach of Voevodsky gives a powerful tool for the study of cohomology theories on algebraic varieties. One can also use this machinery to construct new cohomology theories from old ones, or to break some interesting motives into simpler pieces. We will give a survey of some of the foundations as well as a number of applications.

#### MADHAV NORI University of Chicago

#### Regularisation of infinite series and Analytic Continuation

A simple proof of analytic continuation of certain series obtained by summing over lattices in Euclidean space will be given.

# ARTHUR OGUS University of California

Hodge cohomology of invertible sheaves

Let X/k be a smooth projective scheme over a field k of characteristic zero. For integers i, j and d, let

 $S_d^{i,j} := \{ L \in Pic^0(X) : \dim H^i(X, \Omega^j_{X/k} \otimes L) \ge d \}.$ 

This is a closed subset of  $Pic^{0}(X)$ , and it was conjectured by Beauville and Catanese and proved by Lazersfeld, Green, and Simpson that each of its irreducible components is a translate of a subabelian variety of  $Pic^{0}(X)$  by a torsion point. Pink and Roessler recently

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gave a new proof of this result using reduction modulo p techniques introduced by Deligne and Illusie. I will discuss an attempt (with H. Esnault) to address some remaining issues concerning the behaviour of

$$H^m_{Hdg}(L) := \bigoplus_{i+j=m} H^j(X, \Omega^i_{X/k} \to L),$$

when L has finite order.

#### TAKESHI SAITO University of Tokyo

Wild ramification and the characteristic cycle of an l-adic etale sheaf

The graded quotients of the logarithmic higher ramification groups of a local field of characteristic p¿0 are abelian groups killed by p. Their character groups are canonically embedded in some spaces of twisted differential forms. Using the embeddings, we define the characteristic cycle of an l-adic sheaf, satisfying a certain conditions, as a cycle on the logarithmic cotangent bundle and prove that the intersection with the 0-section gives the characteristic class.

#### CHAD SCHOEN Duke University

Some surfaces of general type in abelian varieties

We discuss two examples of smooth, projective surfaces for which the image under the albanese map cannot be expressed as linear combinations of intersections of divisors.

# VASUDEVAN SRINIVAS Tata Institute of Fundamental Research

#### Oriented intersection multiplicities

Barge and Morel defined a graded "oriented Chow group" of a smooth variety over a field, which may be viewed as a quotient of a group of "oriented algebraic cycles" modulo a suitable equivalence relation. A precursor was the idea of an oriented 0-cycle, suggested by M. Nori, which led to the Euler class group, considered in works of Raja Sridharan, S. M. Bhatwadekar, S. Mandal, and others.

Fasel constructed an intersection product on the oriented Chow groups of Barge and Morel, leading to an "oriented Chow ring", which admits a graded ring homomorphism to the "usual" Chow ring of (unoriented) cycles. In my lecture, I'll introduce these ideas, and discuss some joint work with Fasel, about the corresponding notion of intersection multiplicities.