

RISK ANALYSIS FOR MARKED POINT PROCESS DATA

David R. Brillinger
Statistics Department
University of California, Berkeley

brill@stat.berkeley.edu www.stat.berkeley.edu/users/~brill

$$2\pi \neq 1$$

$$2\pi \neq 1$$

$$2\pi \neq 1$$

Layout

- 1. Layout
- 2. Introduction
- 3. Some statistical background
- 4. The seismic case
- 5. The wildfire case
- 6. Insurance considerations
- 7. Discussion

Acknowledgements



SUISS OF YOR CATHERDRAL-LIBROR.



BODIES OF THE CHURCH OF ST. PANS-LUBBOR.



RUSSIA OF THE OPERATOR OF LUBOR.



BODING OF THE CHURCH OF ST. PURSUE LIMITE.





2. Introduction.

Risk analyses and (marked) point processes abound

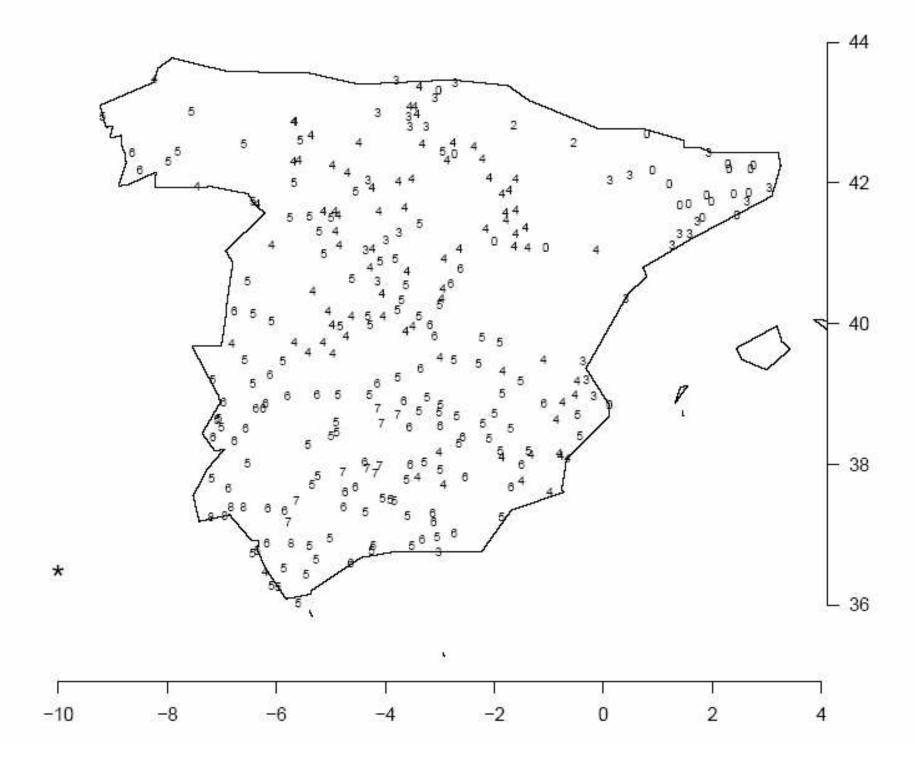
Concern here is with:

earthquakes

wildfires

insurance issues

One specific topic is ordinal-valued marks



A SYNOPSIS OF THE EUROPEAN MACROSEISMIC SCALE (EMS 98)

| EMS | DEFINITION | DESCRIPTION | | | | |
|-----|---------------------|---|--|--|--|--|
| 1 | Not felt | Not felt, even under the most favourable circumstances. | | | | |
| 2 | Scarcely felt | Vibration is felt only by individual people at rest in houses, especially on upper floors of buildings. | | | | |
| 3 | Weak | The vibration is weak and is felt indoors by a few people. People at rest feel a swaying or light trembling. | | | | |
| 4 | Largely observed | The earthquake is felt indoors by many people, outdoors by very few. A few people are awakened. The level of vibration is not frightening. Windows, doors and dishes rattle. Hanging objects swing. | | | | |
| 5 | Strong | The earthquake is felt indoors by most, outdoors by few. Many sleeping people awake. A few run outdoors. Buildings tremble throughout. Hanging objects swing considerably. China and glasses clatter together. The vibration is strong. Top heavy objects topple over. Doors and windows swing open or shut. | | | | |

| 6 | Slightly damaging | | | | | |
|----|------------------------|---|--|--|--|--|
| 7 | Damaging | Most people are frightened and run outdoors. Furniture is shifted and objects fall from shelves in large numbers. Many ordinary buildings suffer moderate damage: small cracks in walls; partial collapse of chimneys. | | | | |
| 8 | Heavily damaging | Furniture may be overturned. Many ordinary buildings suffer damage: chimneys fall; large cracks appear in walls and a few buildings may partially collapse. | | | | |
| 9 | Destructive | Monuments and columns fall or are twisted. Many ordinary buildings partially collapse and a few collapse completely. | | | | |
| 10 | Very destructive | Many ordinary buildings collapse. | | | | |
| 11 | Devastating | Most ordinary buildings collapse. | | | | |
| 12 | Completely devastating | Practically all structures above and below ground are heavily damaged or destroyed. | | | | |

3. Some statistical background.

Planar point process.

locations in the plane of points (x_j, y_j) for j=1,2,3,...

$$Y(x,y) = \sum_{j} \delta(x - x_{j}, y - y_{j})$$

Marked point process.

sequence (x_j, y_j, M_j) for j = 1, 2, 3, ...

Marks may be real, e.g. fire size, seismic damage cost

$$Y(x,y) = \sum_{j} M_{j} \delta(x-x_{j},y-y_{j})$$

Stochastic case - marks assigned randomly to points?

Spatial-temporal point process.

David Vere-Jones (2005). Some models and procedures for space-time point processes. Fields Institute Workshop on Forest Fires and Point Processes

Models for marks. Categories, label j

- i). interval scale: $j \in R$
- ii). ordinal scale: qualitative order spacing does not matter can merge adjacent
- iii). nominal categories: exchangeable

Goals: few parameters, sensitivity, interpretability

Grouped continuous model. Conceptual approach

Latent random variable ζ

$$Y = j$$
 if $\theta_{j-1} < \zeta \le \theta_j$

Multinomial, mle via

$$Prob\{Y = j\} =$$

 $Prob\{Y \neq 1\}Prob\{Y \neq 2 \mid Y \neq 1\}...Prob\{Y = j \mid Y \neq 1,...,j-1\}$

Model $Prob\{Y = j \mid Y \ge j\}$

Explanatory **X**: $\zeta = -\beta^{\tau} \mathbf{X} + \varepsilon$

Cloglog. Extreme value

$$F(\varepsilon) = 1 - \exp\{-e^{\varepsilon}\}$$

$$Prob\{Y=j \mid Y \ge j, \mathbf{X}\} = 1 - \exp\{-e^{\phi_j - \beta^{\mathsf{T}} \mathbf{X}}\}$$

$$Prob\{Y \le j \mid \mathbf{X}\} = 1 - \exp\{-e^{\theta_j - \beta^{\mathsf{T}} \mathbf{X}}\}$$

$$Prob\{Y=j \mid \mathbf{X}\} = \exp\{-e^{\theta_{j-1} - \beta^{\mathsf{T}} \mathbf{X}}\} - \exp\{-e^{\theta_j - \beta^{\mathsf{T}} \mathbf{X}}\}$$

$$e^{\theta_j} = e^{\phi_j} + \dots + e^{\phi_2} + e^{\phi_1}$$

$$j=1,\dots,J-1$$

Chosen X

Estimate of linear predictor

$$\zeta = -\hat{\beta}^{\tau} \mathbf{X} + \gamma, \qquad \gamma = .57721566...$$

Which cell $(\hat{\theta}_{j-1}, \hat{\theta}_j)$ does ζ fall into?

```
Inference.

mle
glm
gam
Besag models
```

Baddeley-Turner's spatstat

Assessment of fit

4. The seismic case.

Intensity data and maps.

Historically very important

The data are ordinal

How to smooth/display?

Have been used numerically. OK?

Attenuation laws

Lisbon 1755.

1 November 1755 - All Saints Day

Magnitude 8.3 to 9.0, several minutes duration

50-70 thousand deaths

Epicentre in Atlantic

Tsunami, fires

Voltaire, Poème sur le désastre de Lisbonne

Week after event, Royal enquiry by Spain

Model.

Y: intensity (mark)

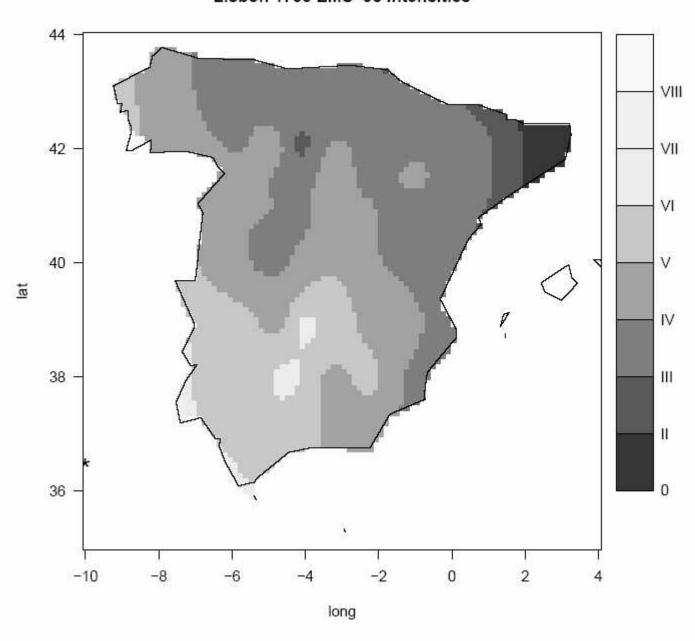
(x,y): location

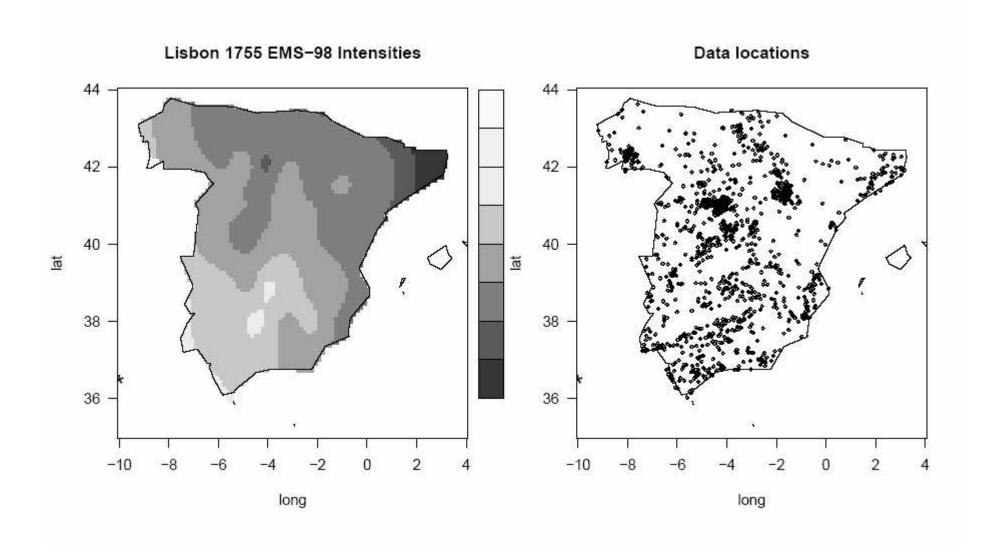
$$Prob\{Y \le j \mid (x,y)\} = 1 - \exp\{-e^{\theta_j - g(x,y)}\}$$

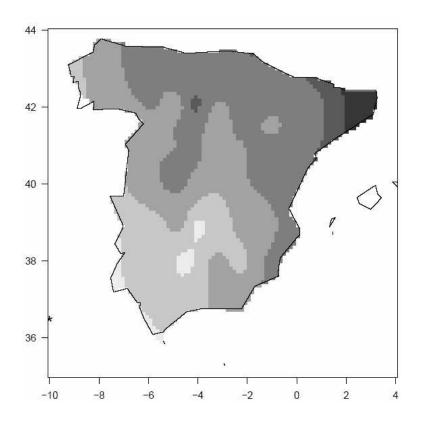
 $\{\theta_j\}$: cutpoints

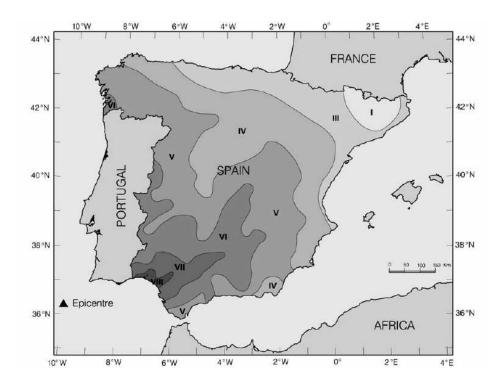
g(x,y): smooth

Lisbon 1755 EMS-98 Intensities

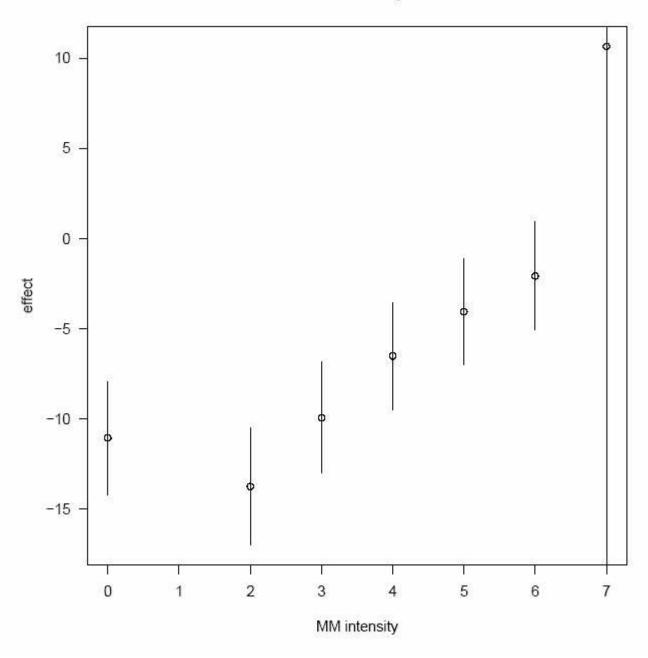








Estimated intensity effects



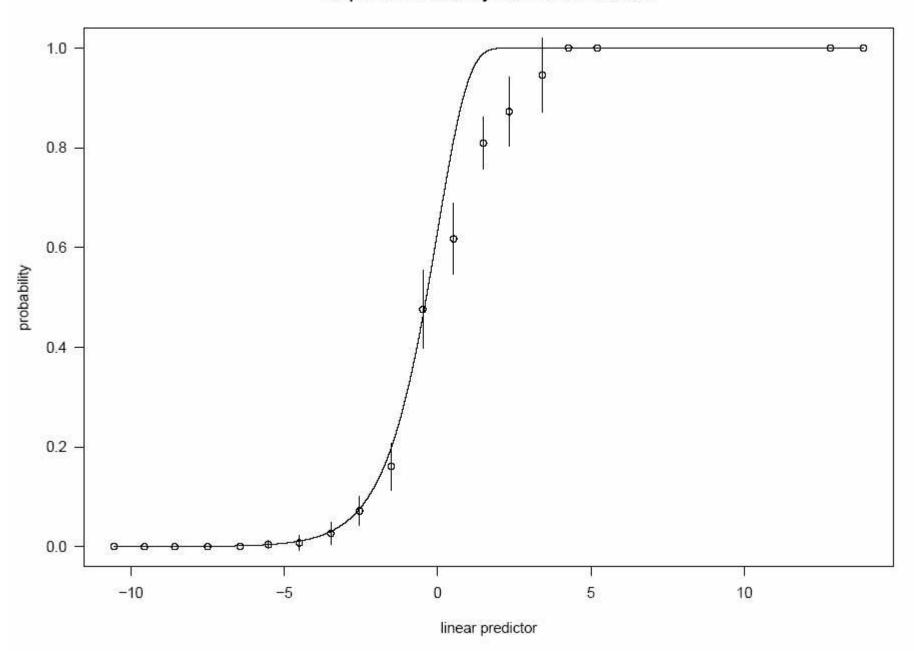
Assessment of fit.

$$Prob\{Y = j \mid Y \ge j, (x,y)\} = 1 - \exp\{-e^{\phi_j - g(x,y)}\}$$

 $\phi_j - g(x,y)$: linear predictor

g(x,y): smooth

Empirical Probability vs. Linear Predictor



$$Prob\{Y = j \mid Y \ge j, (x,y)\} = 1 - \exp\{-e^{\phi_j - g(x,y)}\}$$

 $\phi_j - g(x,y)$: linear predictor

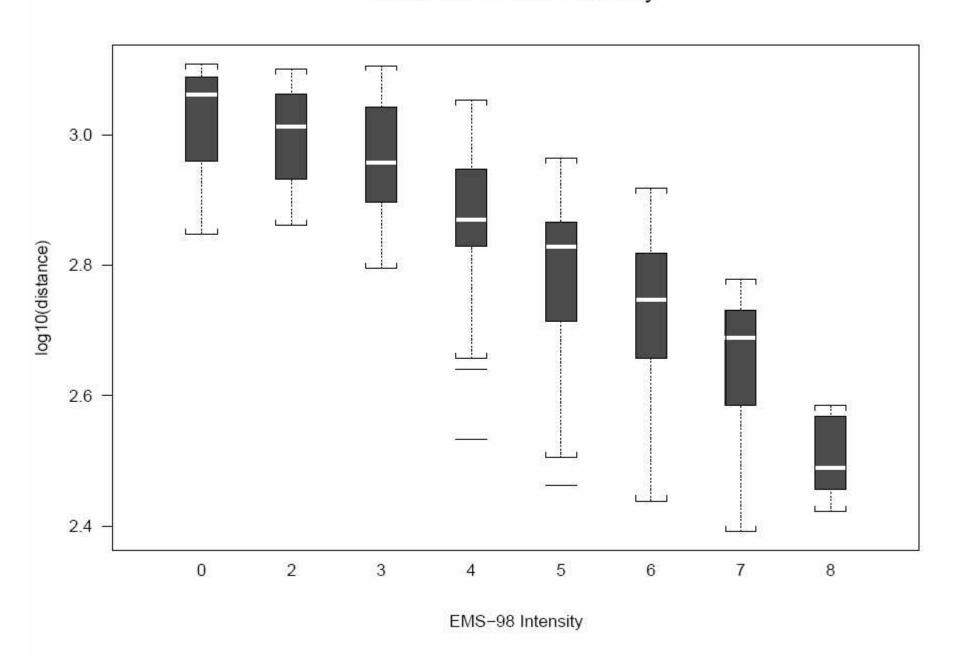
g(x,y): smooth

Parameter estimate uncertainty

Omitted variables, e.g. geology

$$\int \left[1 - \exp\left\{-e^{\phi_j - g(x,y) + \sigma z}\right\}\right] \phi(z) dz$$

Distance versus intensity



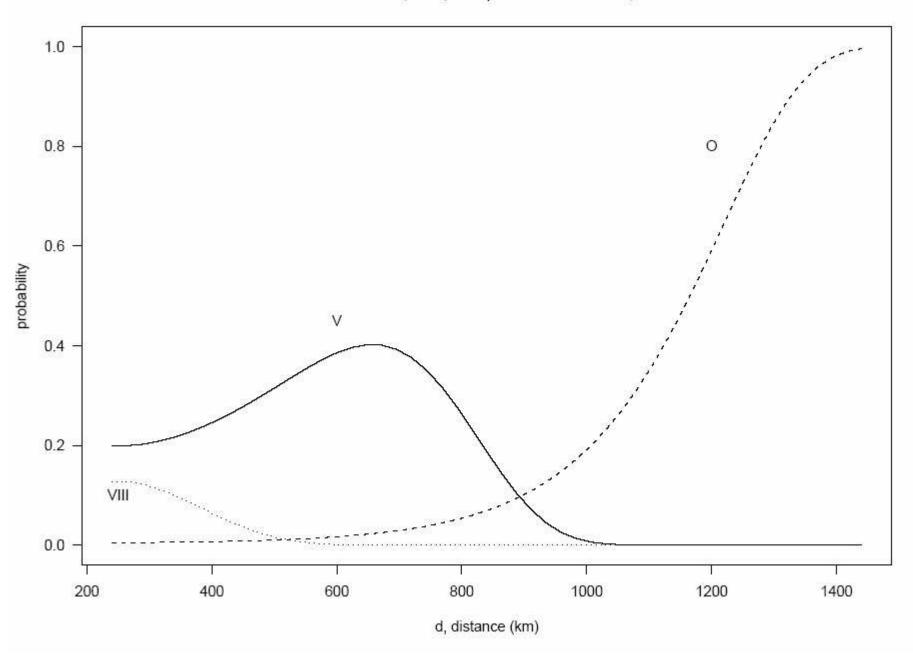
Attenuation.

$$log(-log(1 - Prob\{Y=j\})) = \alpha_j + \beta d + \gamma log(d)$$

d: distance

Needed for building codes

Lisbon: prob{ I = i | source distance }



Damageability matrix.

Two building types

Masonry - traditional houses at the times of the shock Monumental - castles, churches, ...

Proportions damaged

| Risk type vs. EMS-98 | $^{ m V}$ | VI | VII | VIII |
|----------------------|-----------|-----|-----|------|
| masonry | .01 | .25 | .61 | .92 |
| monumental | .04 | .25 | .52 | .60 |

Martinez Solares & Lopez Arroyo (2004)

5. Wildfires.

Tens of thousands/year in North America

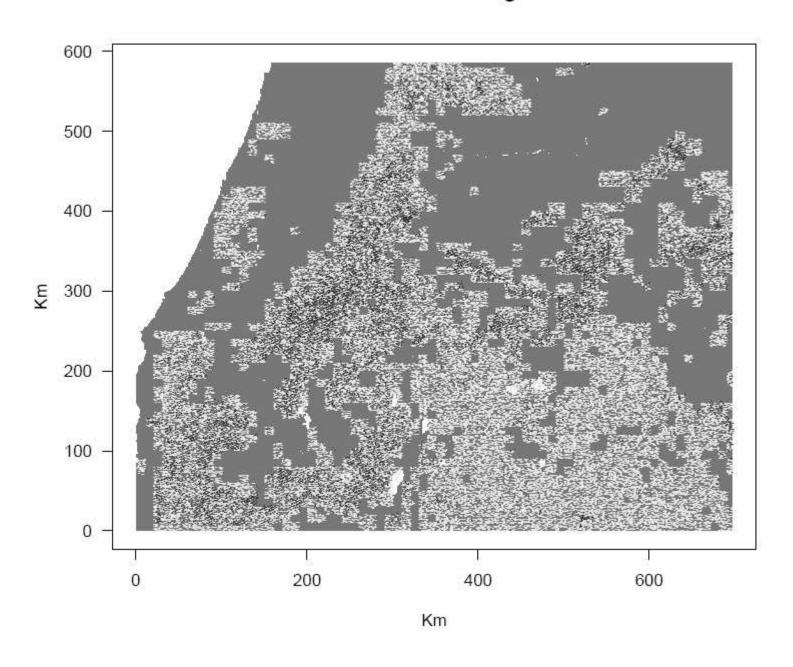
Millions of acres

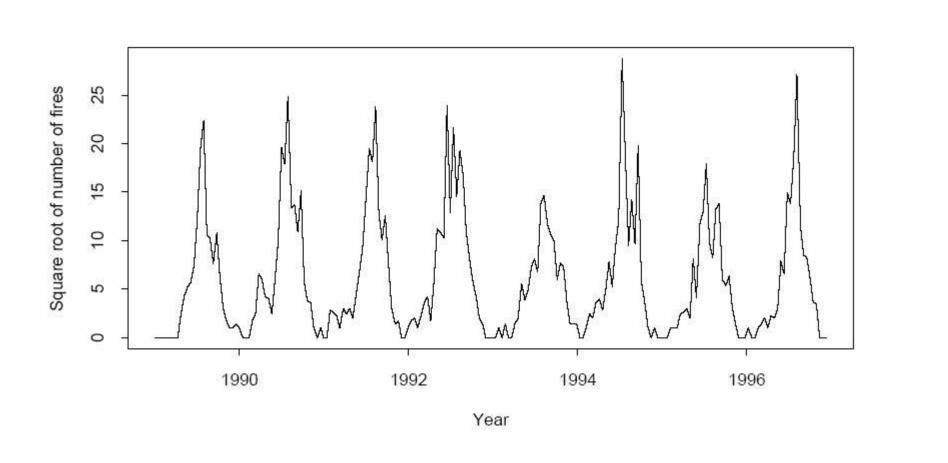
Hundreds millions of dollars spent on suppression

1989 - 1996 date, size, location in Oregon

n = 15,786

Fires in Federal Lands in Oregon 1989 - 1996





Model.

Many voxels, (dx, dy, dt). All "fires", sample of "no-fire" cases (with prob $\pi = .00012$).

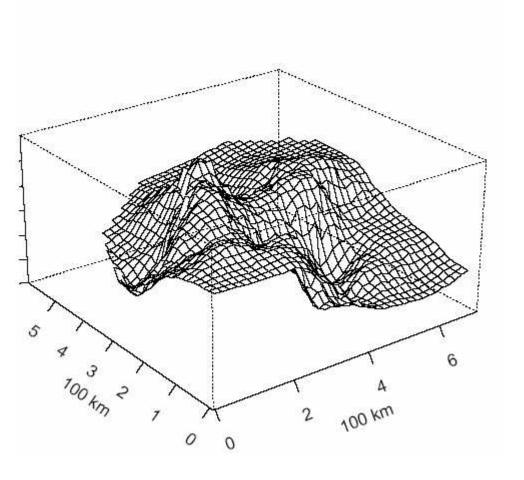
$$logit \ risk = g_1(x,y) + g_2(d) + \zeta$$

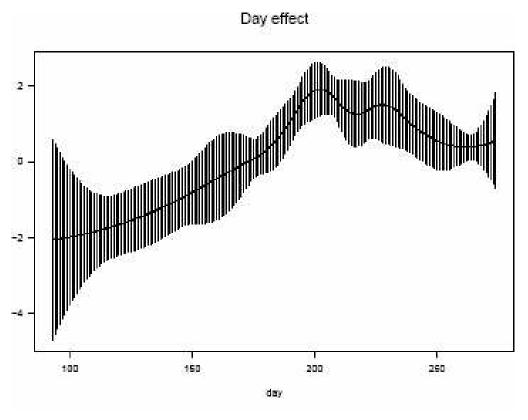
(x,y) - location

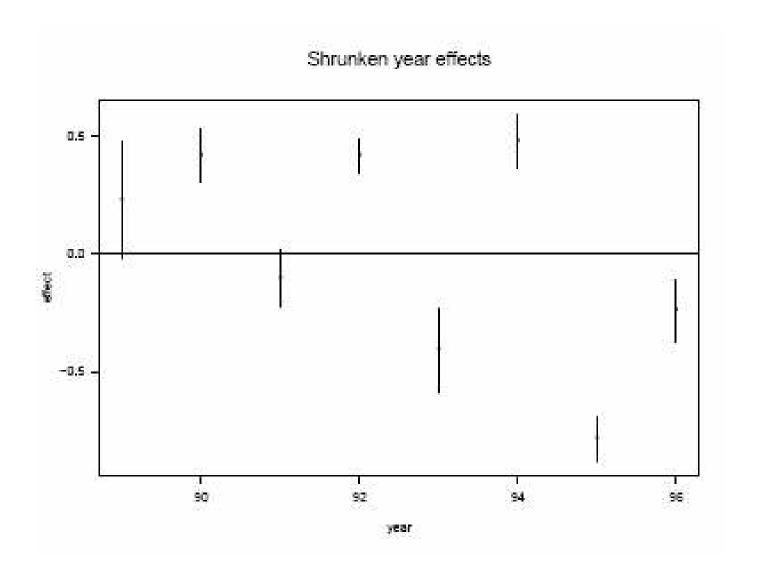
d - day of the year

 ζ - year effect: $IN(0, \tau^2)$

 $\log 1/\pi$ as offset, $\log t p = \log(p/(1-p))$







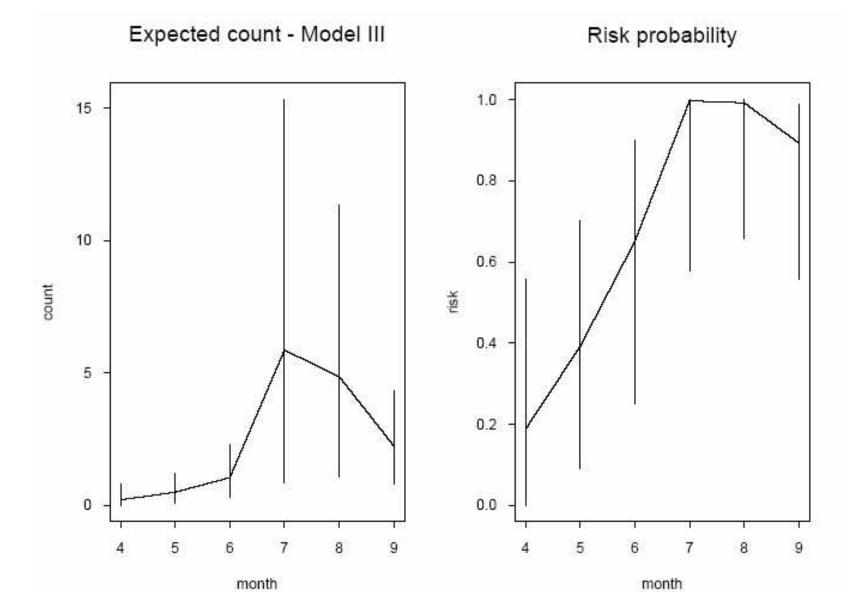
Expected number of fires for some region and future occasion

$$\hat{=} \sum_{i} \int \exp\{\hat{\eta}_{i} + \hat{\tau}z\} / (1 + \exp\{\hat{\eta}_{i} + \hat{\tau}z\}) \phi(z) dz \tag{*}$$

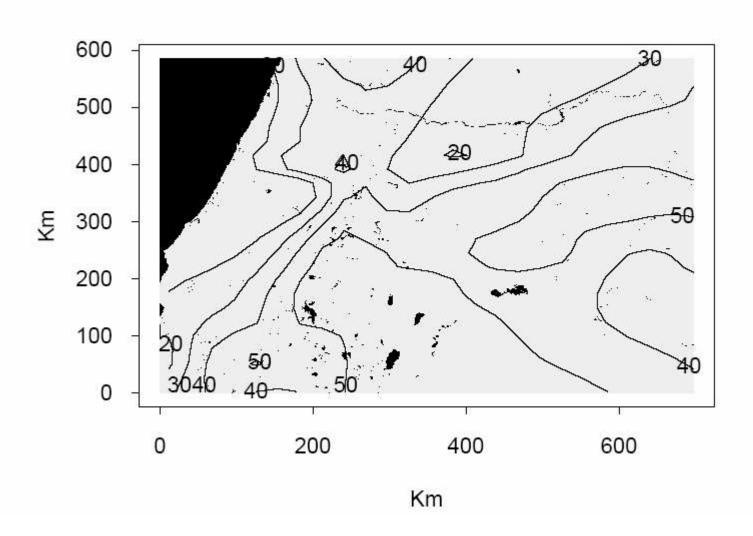
with *i* labelling pixels and days of the month and $\hat{\eta}_i = \hat{g}_1(x_i, y_i) + \hat{g}_2(d_i)$.

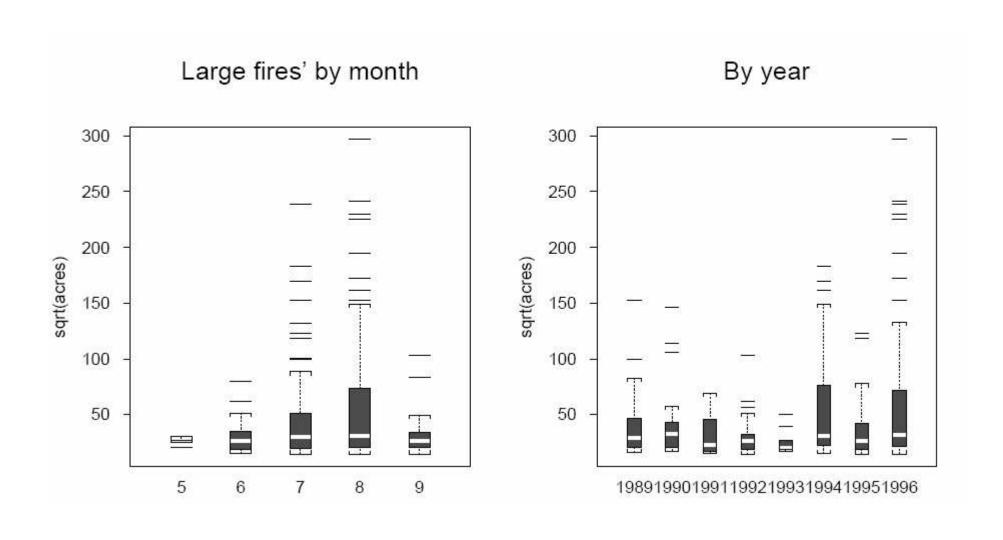
If after

Prob {at at least one fire in M} can integrate/sum (*) over M.

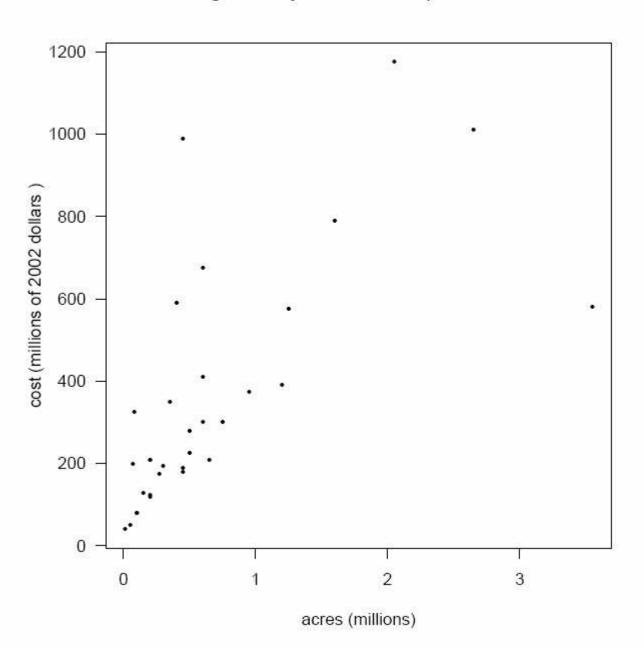


Average fire size (acres)





Damageability relationship for wildfires



6. Insurance considerations.

L: accumulated claims over a year

Pure risk premium.

$$P = E\{L\} = \mu_L$$

Loaded premium. safety premium

$$P = (1+\lambda)\mu_L + \beta\sigma_L + \gamma\sigma_L^2$$

Loading should be larger the greater the uncertainty involved

Damageability matrix/relationship. Provides potential losses from given "intensity"

Discussion.

Considering the insurance problem provides focus

Can treat intensities as approximately numerical

Acknowledgements.

The organizers.

John Braun

David Martell

Rick Schoenberg

B. Bolt, J. M. Martinez Solares, J. Benoit, H. Preisler

NSF Grant DMS-02-03921

US Forest Service Contract 02-JV-11272165-02

- 183. "Some examples of risk analysis in environmental problems keynote talk." Computing Science and Statistics, Volume 34, 3-24 (2002).
- 184. Brillinger, D.R., Preisler, H. K. and Benoit, J. W. "Risk assessment: a forest fire example. Science and Statistics. Pp. 177-196 in Lecture Notes in Statistics 40, IMS (2003)
- 186. "Risk analysis: Examples and discussion (Plenary Talk)." Pp. 3-11 in Applications
- of Statistics and Probability in Civil Engineering (Eds. A. Der Kiureghian, S. Madanat and J. M. Pestura), Millpress, Rotterdam. Vol. 1, Pp. 3-12 (2003)
- 189. "Three environmental probabilistic risk problems", Statistical Science (2003), 412-421.
- 191. Brillinger, D.R., Preisler, H.K. and Naderi, H.M. "Wild fire chances and probabilistic risk assessment". Proceedings of Accuracy 2004 and Ties 2004 Portland, Maine (2004).
- 192. Preisler, H.K., Brillinger, D.R., Burgan, R.E. and Benoit, J. W. "Probability based models for estimation of wildfire risk. Int. J. Wildland Fire 13, 133-142 (2004)
- 197. Brillinger, D. R., Preisler, H. K. and Benoit, J.W. "Probabilistic Risk Assessment for Wildfires". Environmetrics, to appear (2005).