# Integration in Neuroscience from a Cellular-based Neuronal Network Perspective

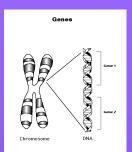
Frances K. Skinner
Toronto Western Research Institute
University Health Network and
University of Toronto

Applications of Mathematics in Medicine Workshop, The Fields Institute,
July 28, 2003

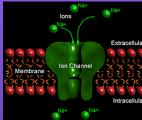
#### TALK OUTLINE

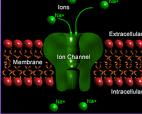
- General introduction
- Hippocampus focus
- Experimental data focus
- Basket cell focus
- Modelling approach 1 simulations and ad-hoc analyses (synaptic depression)
- Modelling approach 2 simulations and linking to experimental data (gap junctions)
- Closing

#### Behavioural State

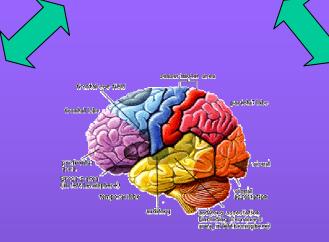




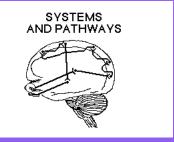






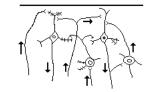


*Interacting dynamics* **Bidirectionality** 

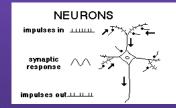




LOCAL NETWORKS







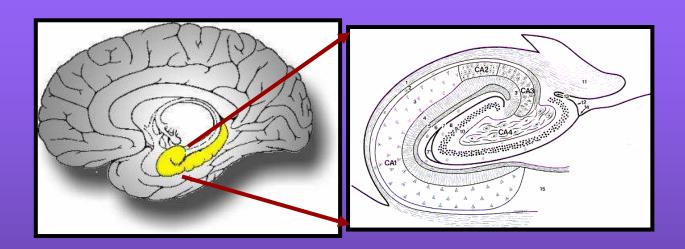


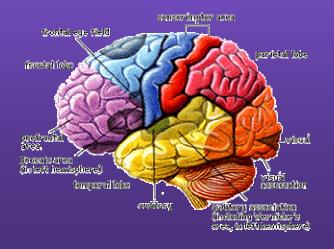
SYNAPSES

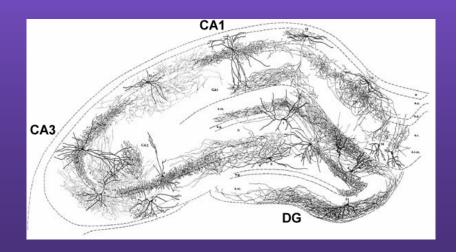


# Focus and Context

### "Welcome to the hippocampal world!"



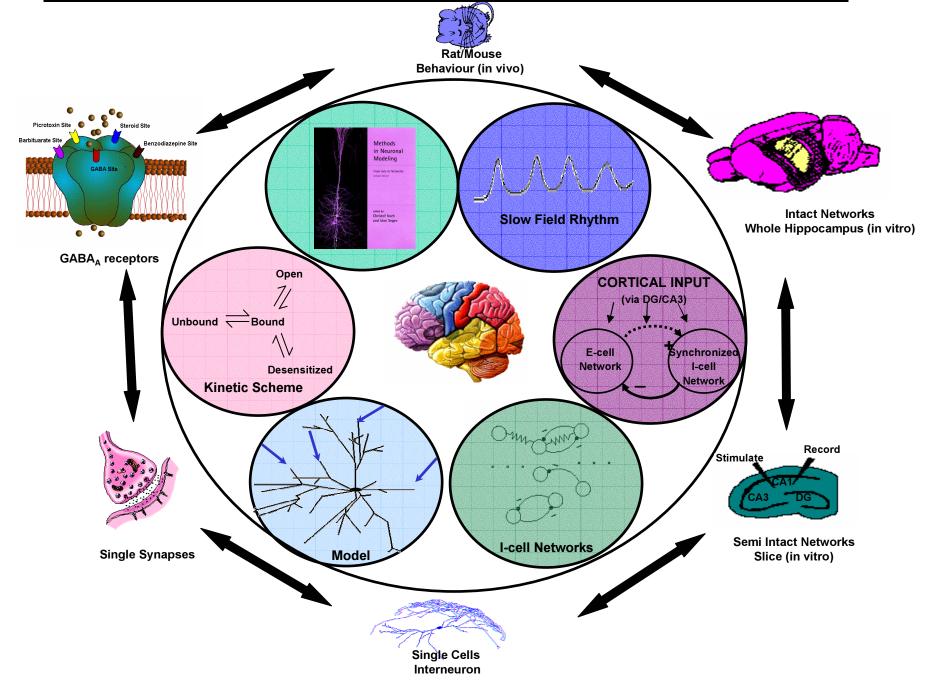




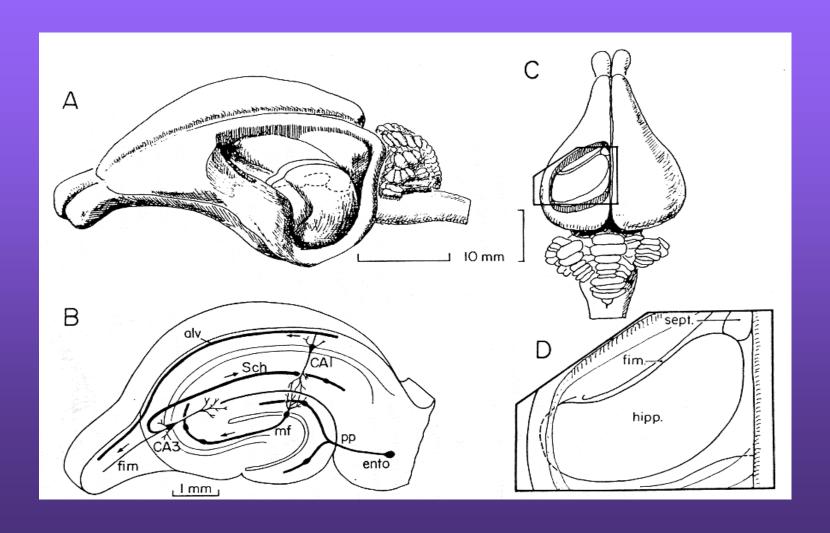
# The hippocampal cortex is an intensely studied region of the brain because:

- It is amenable to experiment, retaining its synaptic circuitry and thus population activities in the slice.
- It is associated with memory and learning (i.e., LTP, LTD), epileptic seizures, and neurogenesis.
- It exhibits a wide range of population activity patterns (<1 to >200 Hz) that are associated with various behavioural states.

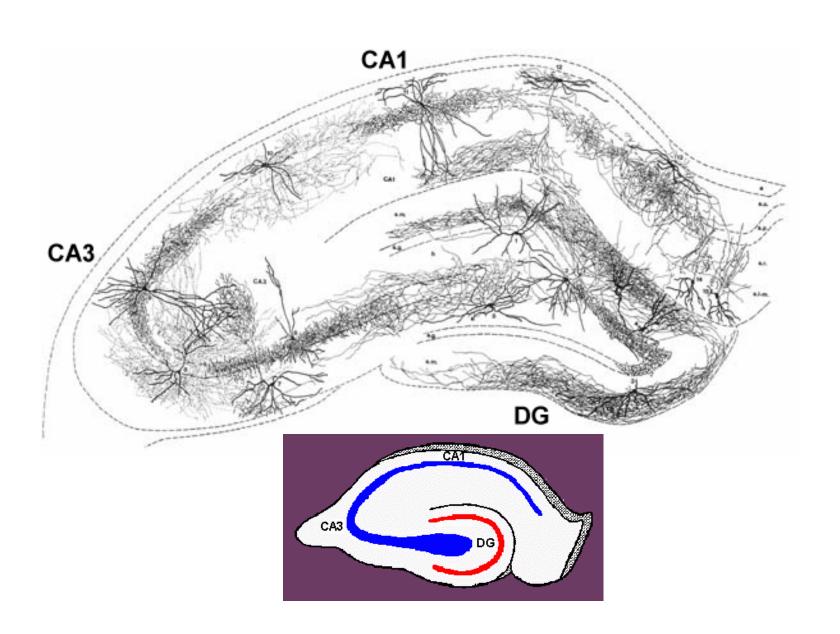
#### "Computational Road Maps to Dynamic Phenotypes"



#### Hippocampus and conventional slice preparation



### Layers, signal flow, cell types



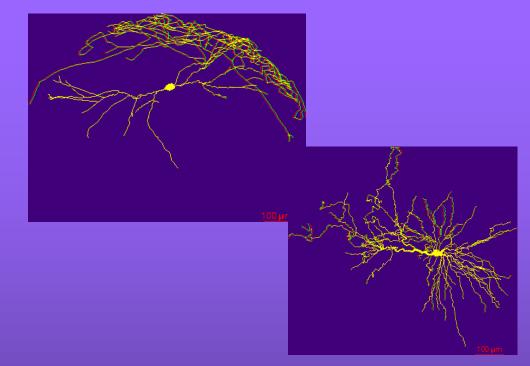
#### Interneurons

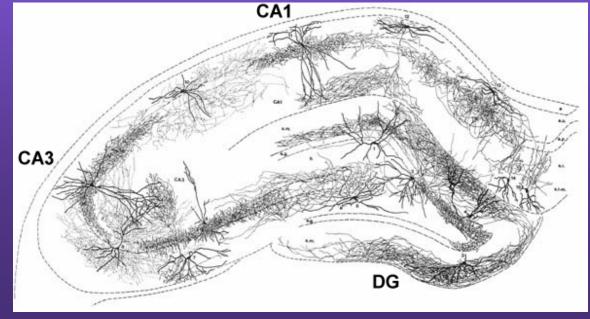
(GABAergic nonprincipal cells or Inhibitory neurons)

"Interneurons are part of an extensive inhibitory network which play an essential role in molding the synchronous rhythmic output of principal cells."

Freund and Buzsáki, Hippocampus 6:347-470, 1996

Interneurons
represent 10-20%
of the neuronal
population but may
provide the precise
temporal structure
necessary for
ensembles of
neurons to perform
specific functions.

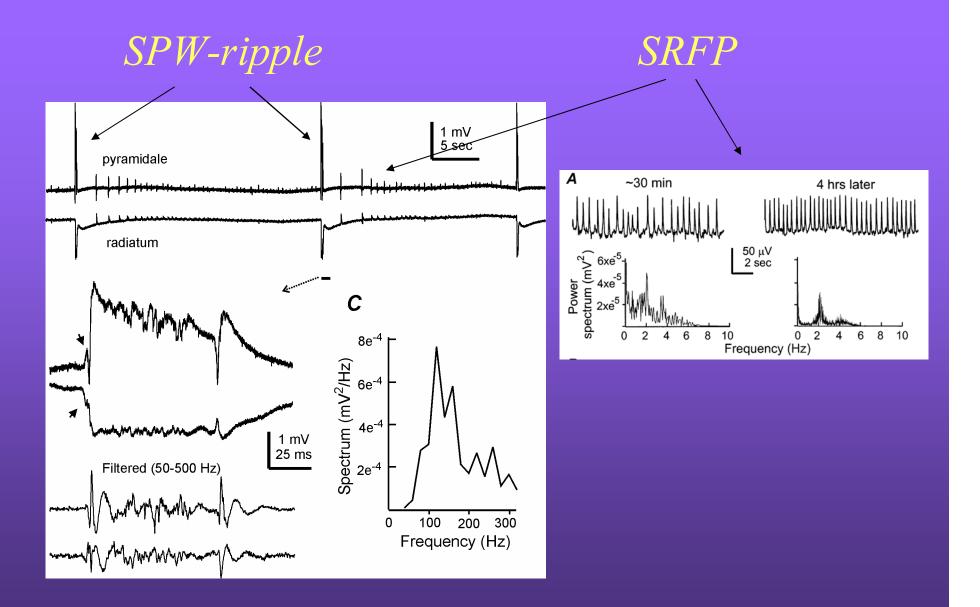




Two types of population activities obtained in whole hippocampus and thick slice preparations (...that critically depend on inhibitory cell participation)

• Spontaneous rhythmic field potentials (SRFPs)

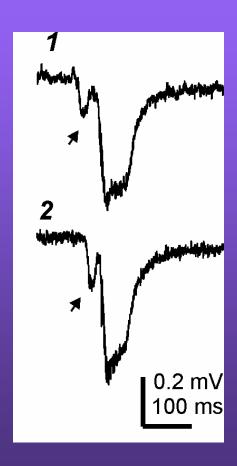
• Sharp wave-ripples (SPW- ripples)



# Stable population activities and relationship between SRFPs and SPWs

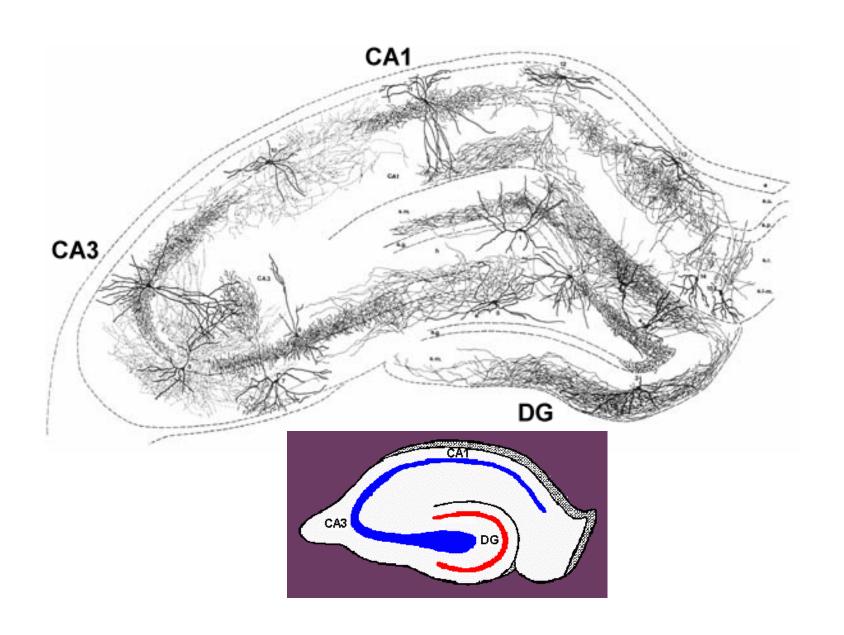
*Initial time* ———

*An hour and a half later* —

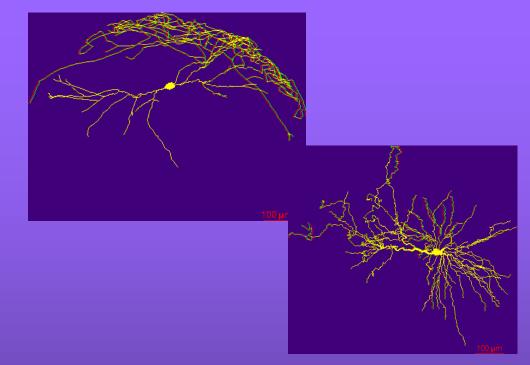


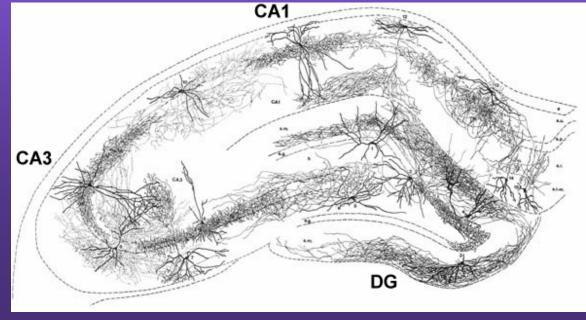
What are the cellular and network mechanisms underlying these population activities? (i.e., interactions between intrinsic and synaptic dynamics need to be understood.)

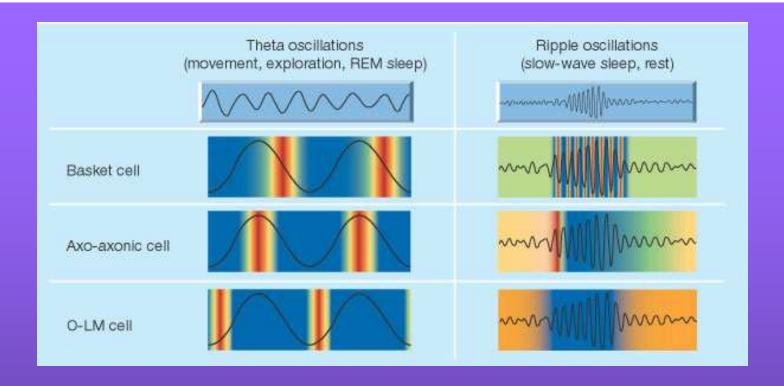
### What model(s) to build?



Interneurons
represent 10-20%
of the neuronal
population but may
provide the precise
temporal structure
necessary for
ensembles of
neurons to perform
specific functions.



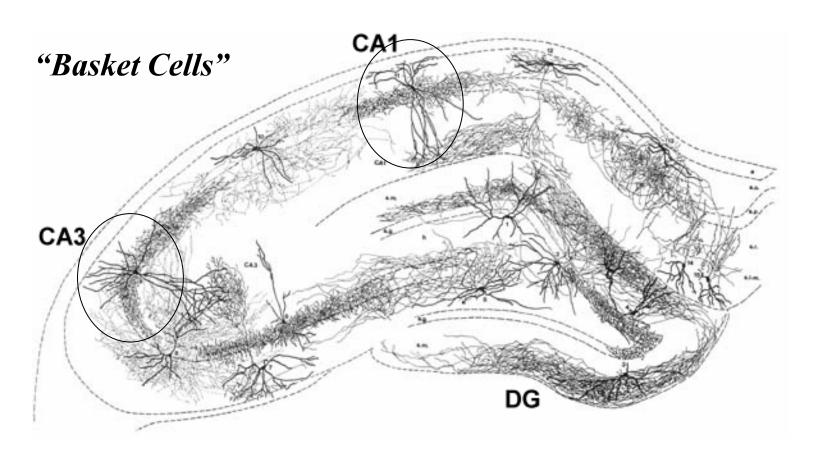




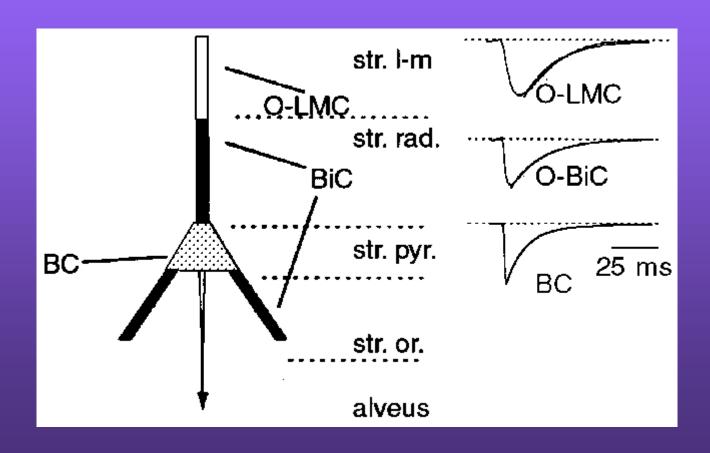
#### Interneurons and electrical oscillations.

Schematic from E.I. Moser, Nature, 2003,
showing the activity profiles of three types of hippocampal
interneurons during two brain states
(based on the findings of Klausberger et al., 2003).
Colours indicate the probability that a given interneuron will fire
(maximum red, minimum blue). The variation within each group is small,
suggesting that classes of interneurons exert precise control
over distinct aspects of hippocampal network dynamics

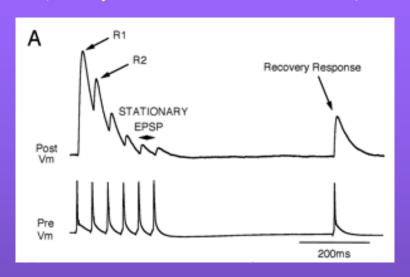
Parvalbumin-containing GABAergic interneuronal networks may be a fundamental structure of the cerebral cortex (Fukuda and Kosaka, 2000)

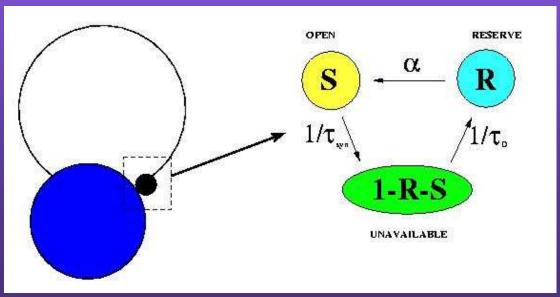


# Basket cells (BCs) exhibit synaptic depression (Maccaferri et al., 2000)

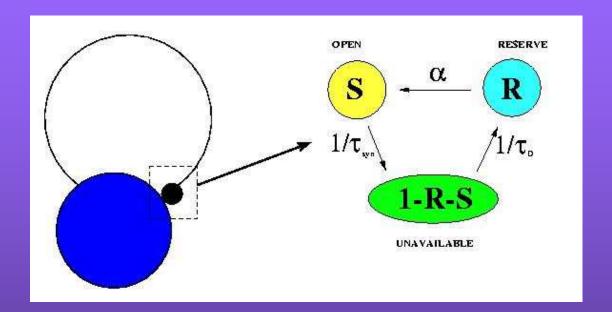


# Short-term Plasticity: phenomenological model (Tsodyks and Markram, 1997)





#### Synaptic Depression (short-term plasticity) model

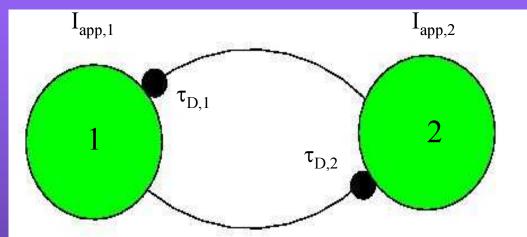


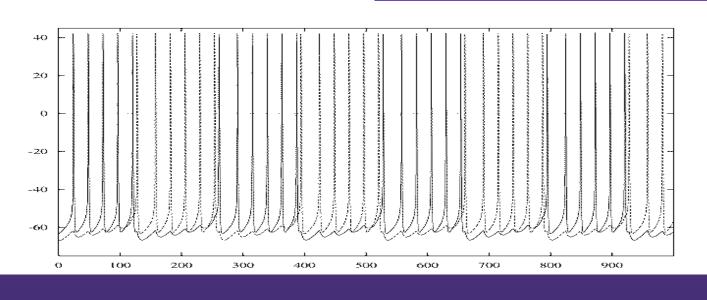
$$I_{syn} = \bar{g}_{syn} S (V - V_{syn})$$
 where 
$$\frac{dS}{dt} = U_{SE} F(V_{pre}) R - \frac{S}{\tau_S}$$
 
$$\frac{dR}{dt} = \frac{1 - S - R}{\tau_D} - U_{SE} F(V_{pre}) R$$
 and 
$$F(V_{pre}) = 1/(1 + \exp(-(V_{pre}))$$

R is the synaptic resource in its recovered state S is the active or effective synaptic resource  $U_{SE}$  is the utilization of synaptic efficacy

#### "Novel Bursting Patterns Emerging from Model Inhibitory Networks with Synaptic Depression"

Jalil, Grigull and Skinner, submitted





#### Intrinsic Properties

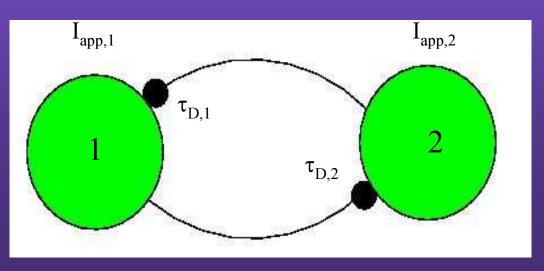
$$C \frac{dV}{dt} = I_{app} - [\bar{g}_{Na} m_{\infty}^{3} h (V - V_{Na}) + \bar{g}_{K} n^{4} + \bar{g}_{L} (V - V_{L}) + I_{syn}]$$

Full two-cell system would be a 10-dimensional Nonlinear system of ODEs

#### **Synaptic Properties**

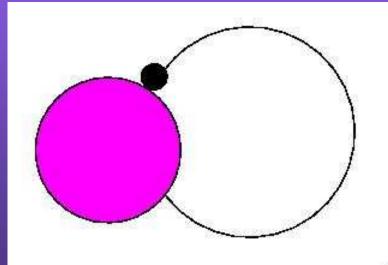
$$I_{syn} = \bar{g}_{syn} S (V - V_{syn})$$
where
$$\frac{dS}{dt} = U_{SE} F(V_{pre}) R - \frac{S}{\tau_S}$$

$$\frac{dR}{dt} = \frac{1 - S - R}{\tau_D} - U_{SE} F(V_{pre}) R$$
and
$$F(V_{pre}) = 1/(1 + \exp(-(V_{pre}))$$



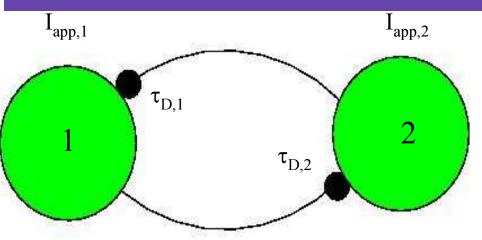
#### Use a strategy of embedding and extrapolation....

$$C \frac{dV}{dt} = I_{app} - [\bar{g}_{Na} m_{\infty}^{3} h (V - V_{Na}) + \bar{g}_{K} n^{4} + \bar{g}_{L} (V - V_{L}) + I_{syn}]$$

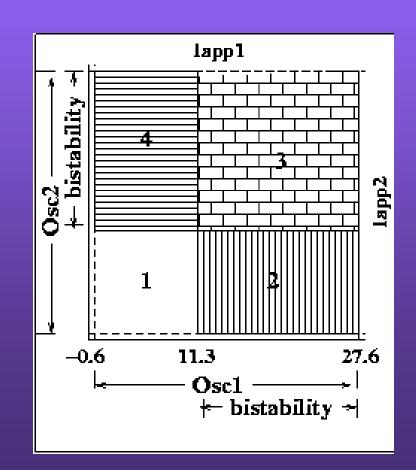


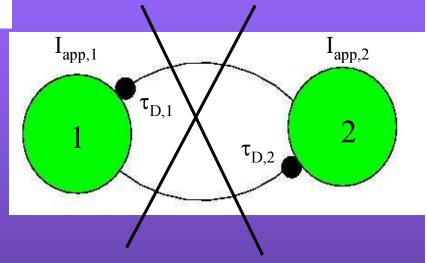
$$I_{syn} = \bar{g}_{syn} S (V - V_{syn})$$
where
$$\frac{dS}{dt} = U_{SE} F(V_{pre}) R - \frac{S}{\tau_S}$$

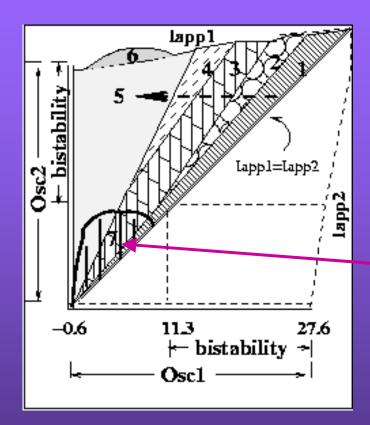
$$\frac{dR}{dt} = \frac{1 - S - R}{\tau_D} - U_{SE} F(V_{pre}) R$$
and
$$F(V_{pre}) = 1/(1 + \exp(-(V_{pre}))$$

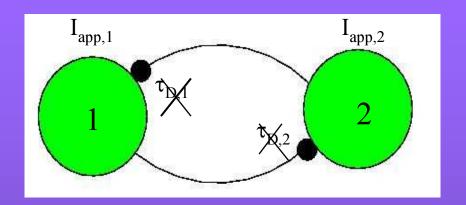


$$C \frac{dV}{dt} = I_{app} - [\bar{g}_{Na} m_{\infty}^{3} h (V - V_{Na}) + \bar{g}_{K} n^{4} + \bar{g}_{L} (V - V_{L}) + I_{syn}]$$

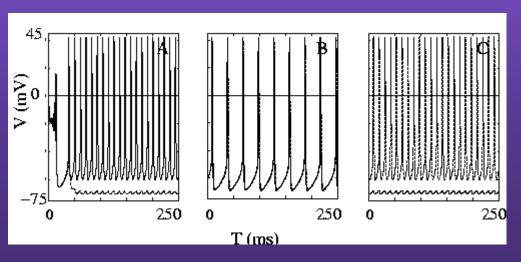


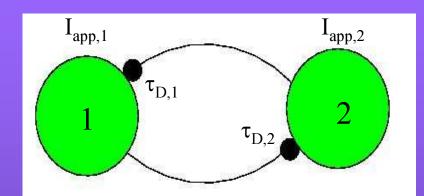


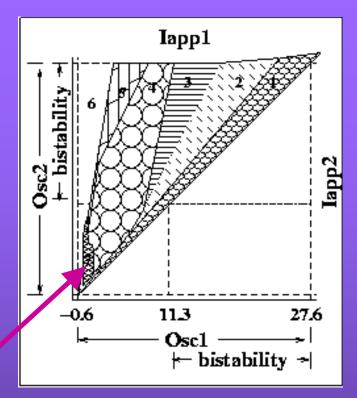


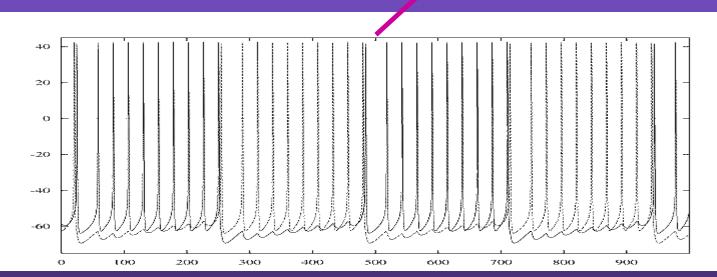


#### "Tristability"



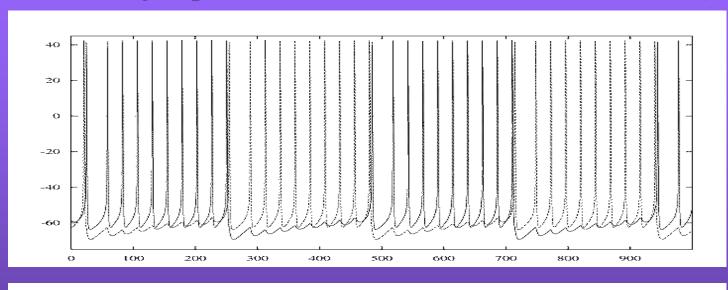


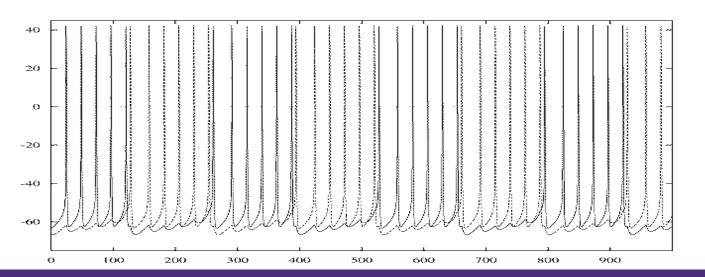




### "Alternating Bursting Pattern"

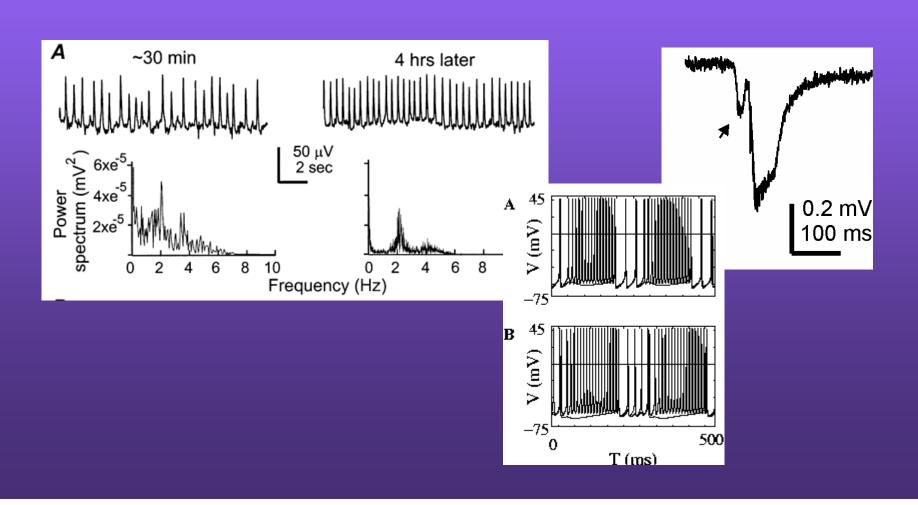
(increasing depression time constant, 300 to 400 msec)



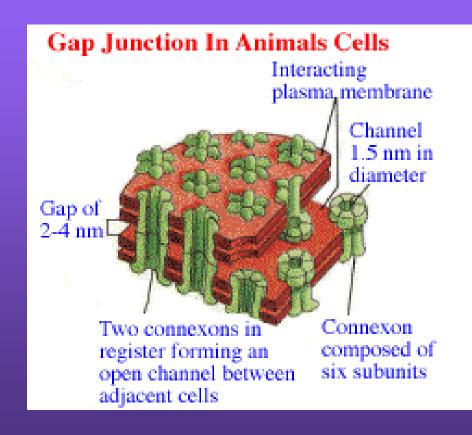


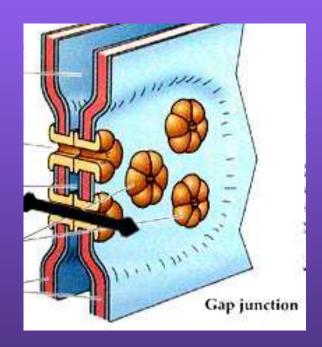
# SRFP and relationship between SRFPs/SPWs:

Speculation and Suggestions from Modelling Work



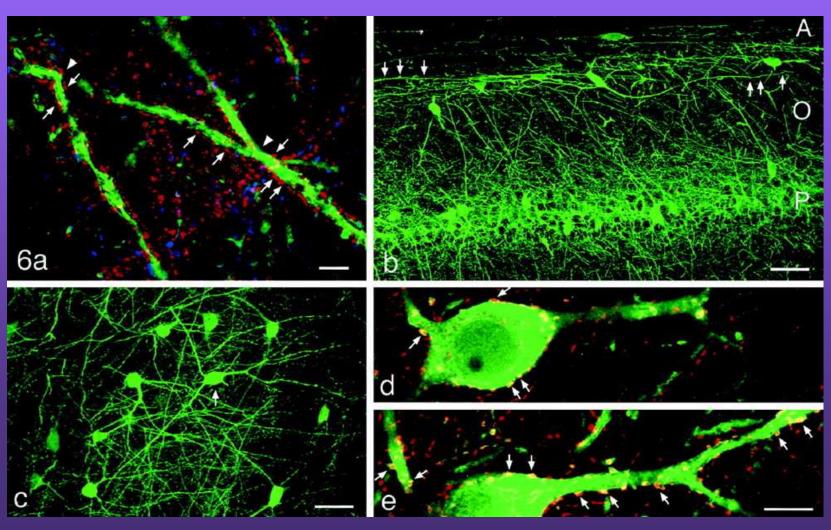
# In addition to chemical inhibitory synapses, electrical connections or gap junctions (GJs) are also present between basket cell inhibitory networks



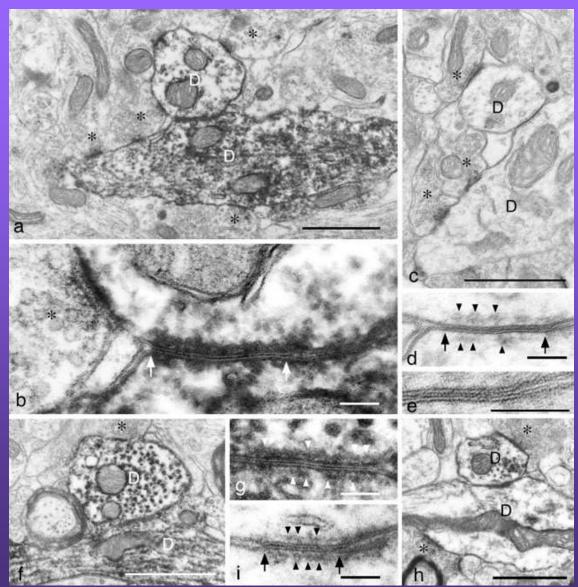


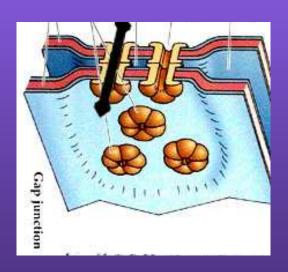
# Hippocampal GABAergic neurons form dual networks connected by chemical (axosomatic) and electrical (dendrodendritic) synapses

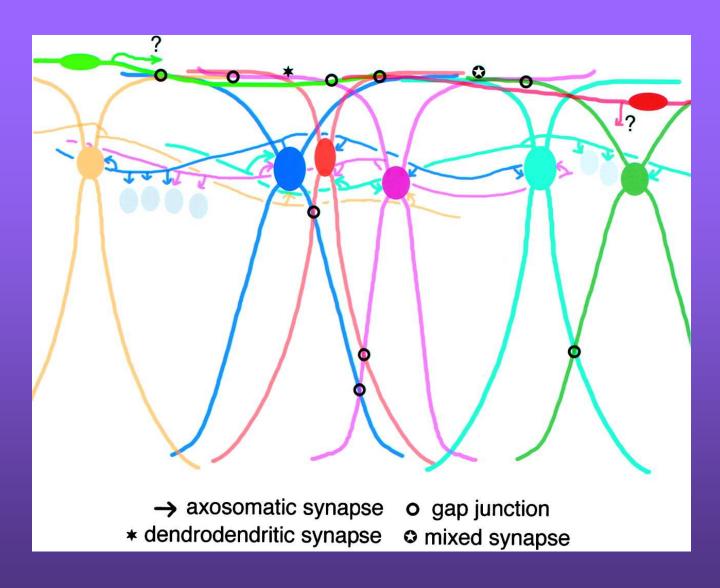
Fukuda and Kosaka, J.Neurosci. 20:1519-1528, 2000



#### Dendrodendritic Gap Junctions







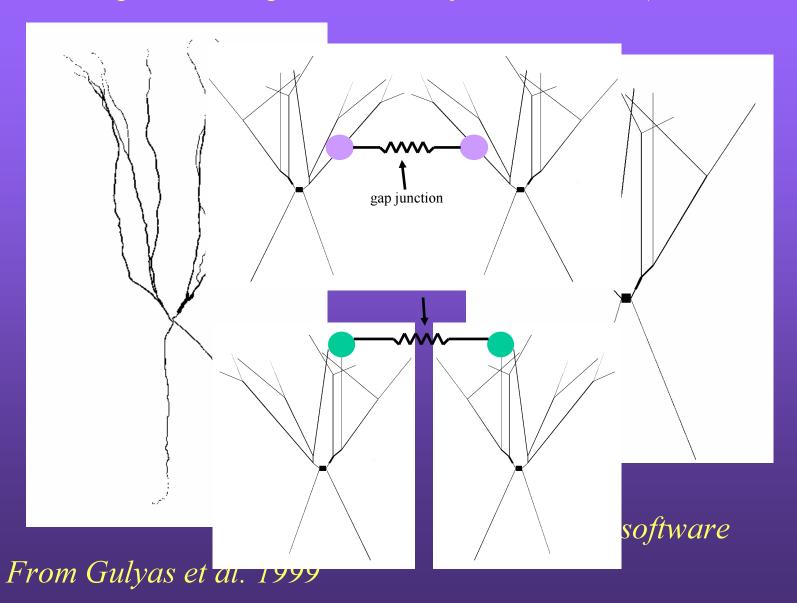
Fukuda and Kosaka, J.Neurosci. 20:1519-1528, 2000

Theoretical and modeling studies using simple neuronal caricatures clearly show that the effects of gap-junctional coupling are not straightforward.

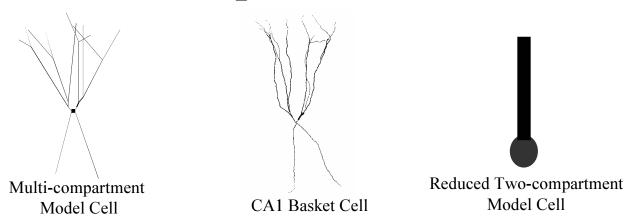
Synchronous, anti-synchronous, phase-locked and bistable patterns can be produced in GJ-coupled networks depending not only on GJ strength, but also on details of the spike shape and frequency.

# What parameter regimes are physiologically relevant?

#### Multi-compartment representation of interneurons (basket cells)



### Ad-hoc Reduced Two-compartment Models

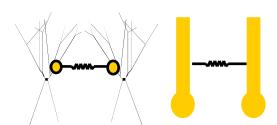


• A two-compartment model was constructed using the following equations:

$$C\frac{dV_S}{dt} = I_{app} - I_{Na} - I_K - I_L - g_{coupD-S}(V_S - V_D)$$

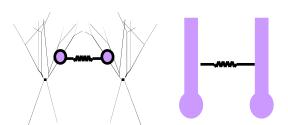
$$C\frac{dV_D}{dt} = -I_L - g_{coupS-D}(V_D - V_S) - I_{gap}$$

#### Two-cell Network Models



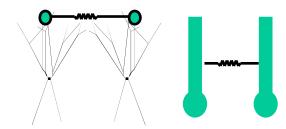


( $\sim$ 100  $\mu m$  from soma)



Middle Location

 $(\sim 200 \ \mu m \text{ from soma})$ 



Distal Location

( $\sim$ 400  $\mu m$  from soma)

- Two-cell (homogeneous) networks of model cells coupled by GJs were constructed where the GJ current for cell i,  $I^{i}_{gap}$ , is given by  $I^{i}_{gap} = g_{gap}(V^{i}_{D} V^{j}_{D})$  where  $i \neq j$ .
- Two-cell networks of the reduced model cells correspond to GJs being located at the selected sites in the full multi-compartment model.

#### Protocol



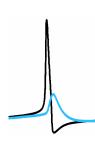
Create multi-compartment model.



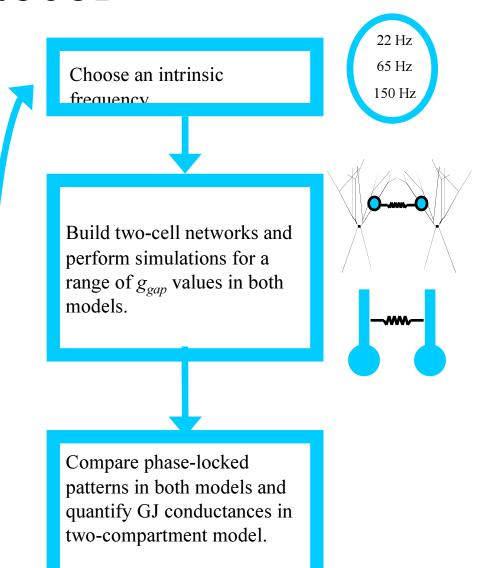
Create two-compartment model such that the passive properties are the same as in the multi-compartment model.



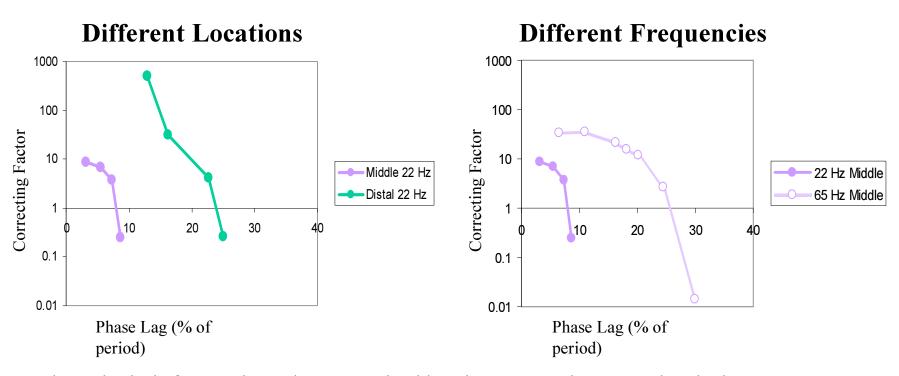
Choose a GJ location in multi-compartment model.



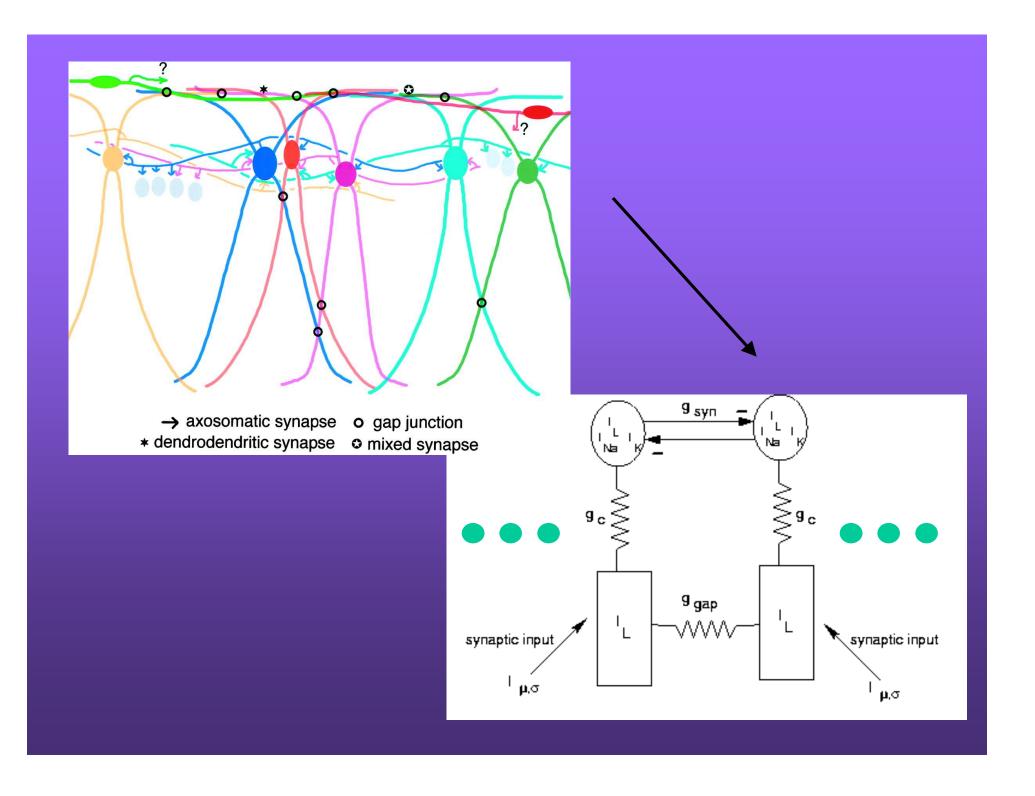
Choose  $g_{coup}$  values for two-compartment model such that the dendritic spike amplitudes are the same in both models.



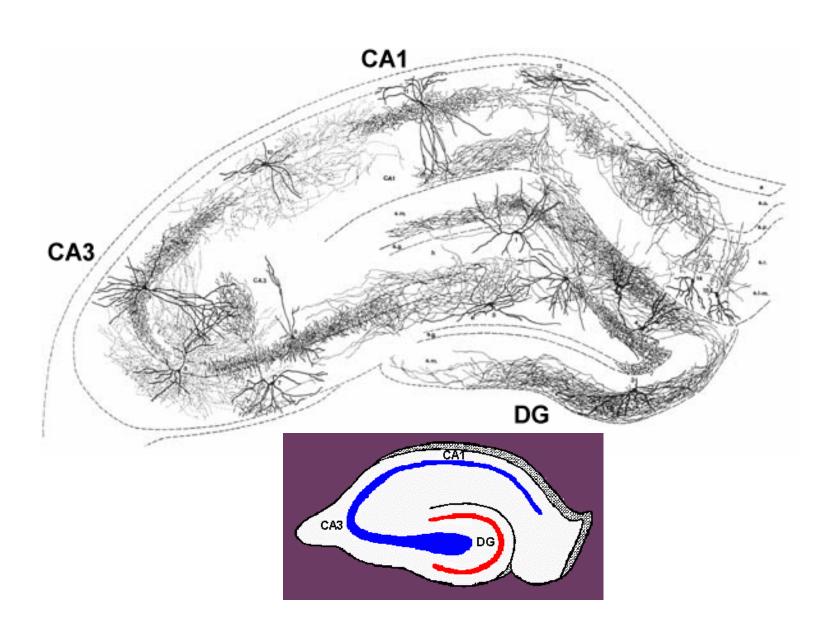
## Quantifying GJ Conductances



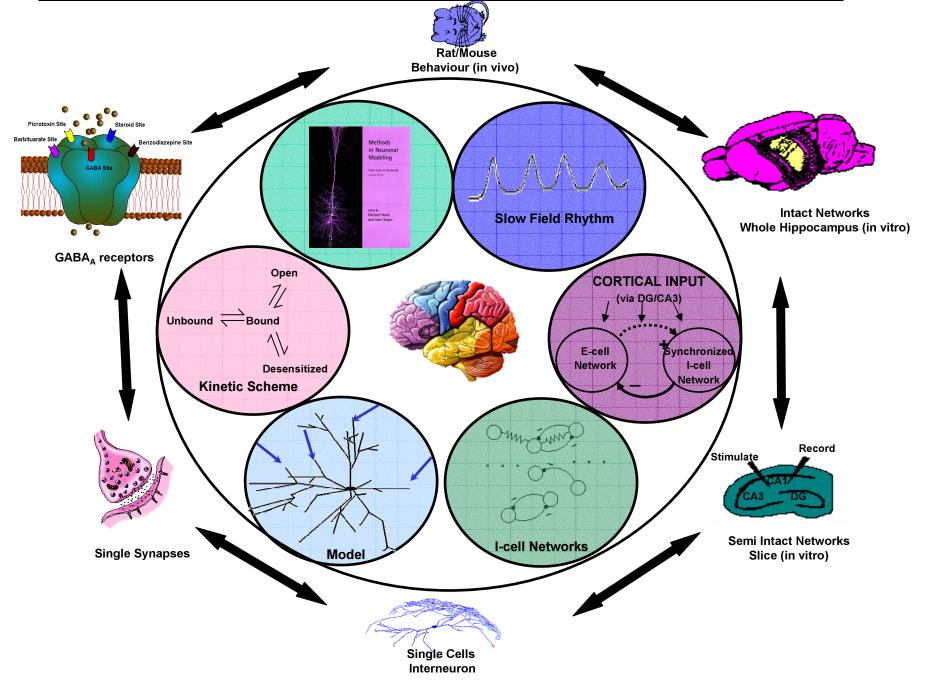
- For lower intrinsic frequencies and more proximal locations, GJ conductance values in the two-compartment models more closely approximate those in the multi-compartment model. The above plots indicate the appropriate correcting factor that needs to be applied.
- In general, when physiological GJ conductances are in the 10 100 pS range, GJ conductances in the two-compartment models are appropriate.



### "Cellular-based network models"



#### "Computational Road Maps to Dynamic Phenotypes"



# Acknowledgements



Dr. Liang Zhang



CIHR (MRC), NSERC, CFI/ORDCF, DCIEM, TWRI/UHN